Shocks in the stacked Sunyaev–Zel’dovich profiles of clusters – I. Analysis with the Three Hundred simulations

Eric J. Baxter,1 Susmita Adhikari,2,3,4 Jesús Vega-Ferrero5,6 Weiguang Cui7,8 Chihway Chang7,9 Bhuvnesh Jain9 and Alexander Knebe10,11,12

1 Institute for Astronomy, University of Hawai‘i, 2680 Woodlawn Drive, Honolulu, HI 96822, USA
2 Kavli Institute for Particle Astrophysics and Cosmology, Stanford University, Stanford, CA 94305, USA
3 Department of Astronomy and Astrophysics, University of Chicago, Chicago, IL 60637, USA
4 Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA
5 IFCA, Instituto de Física de Cantabria (UC-CSIC), Av. de Los Castros s/n, E-39005 Santander, Spain
6 Artificial Intelligence Research Institute (IIIA), Campus UAB, E-08193 Bellaterra, Spain
7 Departamento de Física Teórica, Módulo 15, Facultad de Ciencias, Universidad Autónoma de Madrid, E-28049 Madrid, Spain
8 Institute for Astronomy, University of Edinburgh, Royal Observatory, Edinburgh EH9 3HJ, UK
9 Center for Particle Cosmology, Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, PA 19104, USA
10 Departamento de Física Teórica, Módulo 15, Facultad de Ciencias, Universidad Autónoma de Madrid, E-28049 Madrid, Spain
11 Centro de Investigación Avanzada en Física Fundamental (CIAPP), Facultad de Ciencias, Universidad Autónoma de Madrid, E-28049 Madrid, Spain
12 International Centre for Radio Astronomy Research, University of Western Australia, 33 Stirling Highway, Crawley, Western Australia 6009, Australia

Accepted 2021 September 16. Received 2021 September 16; in original form 2021 January 30

ABSTRACT

Gas infalling into the gravitational potential wells of massive galaxy clusters is expected to experience one or more shocks on its journey to becoming part of the intracluster medium (ICM). These shocks are important for setting the thermodynamic properties of the ICM and can therefore impact cluster observables such as X-ray emission and the Sunyaev–Zel’dovich (SZ) effect. We investigate the possibility of detecting signals from cluster shocks in the averaged thermal SZ profiles of galaxy clusters. Using zoom-in hydrodynamic simulations of massive clusters from the Three Hundred Project, we show that if cluster SZ profiles are stacked as a function of $R_{200}$, shock-induced features appear in the averaged SZ profile. These features are not accounted for in standard fitting formulae for the SZ profiles of galaxy clusters. We show that the shock features should be detectable with samples of clusters from ongoing and future SZ surveys. We also demonstrate that the location of these features is correlated with the cluster accretion rate, as well as the location of the cluster splashback radius. Analyses of ongoing and future surveys, such as SPT-3g, AdvACT, Simons Observatory, and CMB-S4, which include gas shocks will gain a new handle on the properties and dynamics of the outskirts of massive haloes, both in gas and in mass.

Key words: galaxies: clusters: general – galaxies: clusters: intracluster medium – large-scale structure of Universe.

1 INTRODUCTION

In the standard picture of structure formation, gas falling into galaxy clusters experiences one or more shocks before becoming part of the intracluster medium (ICM). The shocking process is essential to the conversion of the kinetic energy associated with infall into the thermal energy of the gas, and is therefore at least partly responsible for setting the thermodynamic properties of the ICM (Evrard 1990). For this reason, shocks are closely connected to our interpretation of cosmological observables tied to the ICM, such as the X-ray and Sunyaev–Zel’dovich (SZ) signals from clusters (e.g. Lau et al. 2015), and the SZ power spectrum. The properties and geometry of cluster shocks are connected to the large-scale cluster environment (Molnar et al. 2009) and to processes like accretion and mergers (Zhang et al. 2020). A better understanding of cluster shocks – in both theory and data – is therefore important both from a cosmological perspective and for understanding how clusters grow and evolve over time. Additionally, cluster shocks are also thought to be sites of cosmic ray acceleration (Kang, Ryu & Jones 1996).

Gas shocks near clusters can be divided into several (not necessarily mutually exclusive) classes depending on their physical origin and properties. Accretion shocks can be defined as the shocks associated with the deceleration of baryons that are infalling into a cluster (Bertschinger 1985). In contrast, merger shocks are generated by the infall of massive substructure merging with the main halo, which can result in an outwardly propagating shock. Recently, Zhang et al. (2020) have pointed out that sufficiently strong merger shocks can propagate to large distances, forming so-called merger-accelerated accretion shocks. Cluster shocks can also be divided into two classes based on their relative location: external and internal shocks. External shocks are associated with pristine, previously unshocked gas, falling on to the cluster and being shocked for the first time (Lau et al. 2015). Internal shocks can result from continued infall of gas after an external shock, from mergers of multiple haloes, and from bulk flows (Molnar et al. 2009). External accretion shocks typically...

* E-mail: ebax@hawaii.edu

© 2021 The Author(s)
Published by Oxford University Press on behalf of Royal Astronomical Society
We note that some authors refer to such external shocks as accretion shocks (e.g. Molnar et al. 2009). Internal accretion shocks are sometimes referred to as virial shocks. Here, we do not attempt to distinguish between the different physical origins of shocks, but rather study their impact on the SZ profiles of galaxy clusters. We focus mainly on external shocks at several virial radii that likely result from merger-accelerated accretion shocks. Recent studies have shown that such shocks are nearly ubiquitous in the outskirts of galaxy clusters (e.g. Aung, Nagai & Lauer 2021; Zhang et al. 2020). For simplicity, we will refer to these as external shocks. We will also occasionally consider internal accretion shocks, i.e. virial shocks.

In spherically symmetric, self-similar models of halo formation, the location of the external shock is related to the current turnaround radius of the cluster (i.e. the radius at which matter stops expanding with the Hubble flow and begins infall towards the cluster) as well as to the halo accretion rate (Bertschinger 1985; Shi 2016). Self-similar models, however, are not expected to describe real clusters for a few reasons. First, the effects of dark energy at late times induce departures from this self-similar picture (Lau et al. 2015). Moreover, in realistic hydrodynamic simulations, where haloes deviate from spherical symmetry and accretion is not smooth, the shock geometry can be complicated, with shocks having different radii depending on direction (e.g. Evrard 1990; Skillman et al. 2008; Molnar et al. 2009; Power et al. 2020).

While external shocks have long been predicted by theory and simulations, detection of these shocks around galaxy clusters in data is complicated by the low density of gas in the cluster outskirts. X-ray observations of thermal bremsstrahlung emission from clusters, for instance, scales as the square of the gas density, making its detection in cluster outskirts challenging (Reiprich et al. 2013). X-ray and \( \gamma \)-ray emission is also expected from cluster shocks as a result of electrons being highly accelerated in the shock fronts and inverse Compton scattering with cosmic microwave background (CMB) photons (e.g. Loeb & Waxman 2000). Detection in \( \gamma \)-rays is challenging because of the small number of photons produced by the shocks and the low resolution of \( \gamma \)-ray telescopes (Keshet et al. 2003). There have been several reported detections of gamma-ray rings associated with cluster virial shocks around individual clusters (e.g. Keshet et al. 2017; Keshet & Reiss 2018), as well as in stacked gamma-ray observations (Reiss & Keshet 2018). The electrons accelerated in shock fronts can also produce a synchrotron signal in the radio (Brunetti & Jones 2014).

A promising avenue for detecting cluster shocks is via the thermal SZ effect (Sunyaev & Zeldovich 1972). The SZ effect is caused by inverse Compton scattering of CMB photons with hot electrons, leading to a spectral distortion of the CMB. The amplitude of the SZ spectral distortion, typically expressed in terms of the Compton \( y \) parameter, is proportional to a line-of-sight integral of the electron gas pressure. Unlike X-ray observations – which are sensitive to the square of the gas density – the TSZ scales linearly in the gas density, making it a powerful probe of gas in the cluster outskirts where shocks are expected (e.g. Kocsis, Haiman & Frei 2005). Kocsis et al. (2005) and Molnar et al. (2009) have shown that the shock radius in simulated clusters is associated with a rapid change in the pressure profiles of these objects, which in turn leads to an SZ signal that could be identified in high-resolution observations from e.g. ALMA.

Several attempts have been made at detecting the SZ signatures from cluster shocks in data. Basu et al. (2016) report a detection of a cluster merger shock using high-resolution observations with ALMA. Similar measurements have been made by Ueda et al. (2018) and Di Mascolo, Churazov & Mroczkowski (2019). Hurier, Adam & Keshet (2019) claim detection of a virial shock around Abell 2319 using much lower resolution, and lower sensitivity Planck data. Keshet, Reiss & Hurier (2020) report that measurements of virial shocks in the SZ are coincident with signals found in gamma-rays.

In this work, we investigate the observational prospects for identifying shock features in SZ observations around large cluster samples from current and future wide-field SZ cluster surveys. Ongoing and planned CMB surveys – including SPT-3G (Benson et al. 2014), AdvACT (Henderson et al. 2016), Simons Observatory (Ade et al. 2019), and CMB Stage 4 (CMB-S4; Abazajian et al. 2016) – will map large fractions of the submillimetre sky to sensitivities 10–30 times higher than the Planck satellite (Aghanim et al. 2016), and with better angular resolution. Furthermore, unlike ultra-high-resolution observations e.g. ALMA, these wide-field surveys will naturally obtain measurements to very large cluster-centric radii with their wide fields of view. Given that these surveys are expected to detect many tens of thousands of galaxy clusters (Abazajian et al. 2016) it is useful to consider whether we can detect shock features around these clusters, and what we can learn from such measurements.

As we show below, we are unlikely to obtain high significance measurements of external shocks around individual clusters with current and near-term wide-field SZ survey data. However, by combining measurements from many clusters, it may be possible to enhance the signal to noise. We show that although there is significant scatter in shock positions and amplitude from cluster to cluster, the \( y \) profile averaged over many clusters does contain distinct features connected to external shocks, and that these features are detectable with near-term surveys.

External shocks form in some sense the boundary of the gaseous component of the halo, separating infalling gas from the higher temperature gas inside shock boundary. Analogous to the gas boundary, the dark matter (DM) component has a boundary at the splashback radius, i.e. the surface formed by the apocentres of the most recently accreted particles (Adhikari, Dalal & Chamberlain 2014; Diemer & Kravtsov 2014; More, Diemer & Kravtsov 2015; Shi 2016). In an idealized spherical solution there is a density caustic at this location (Fillmore & Goldreich 1984; Bertschinger 1985). Self-similar collapse solutions predict that the location of the external shock and the DM caustic coincide for moderately accreting haloes when the gas has an adiabatic index of \( \gamma = 5/3 \), with the shock radius decreasing with accretion rate and increasing with adiabatic index (Shi 2016). Realistic hydrodynamical simulations, however, find that the shock can extend much further outside the splashback boundary of a halo (e.g. Lau et al. 2015). As both the shock radius and the splashback radius correlate strongly with the accretion rate of the halo, self-similar models and hydrodynamical simulations...
simulations both predict that the cluster shock and splashback radii are correlated (Bertschinger 1985; Lau et al. 2015; Shi 2016; Walker et al. 2019; Aung et al. 2021). Hurier et al. (2019) use a comparison between the measured shock and splashback radii of a massive, low-redshift cluster detected by Planck to derive a constraint on the gas adiabatic index. The boundary of the gas component and its relation to the DM boundary is relevant to understanding galaxy evolution in clusters, as this boundary delineates the onset of intracluster processes. We investigate correlations between shock features in the cluster-averaged SZ profiles and the cluster splashback radius. This correlation is potentially measurable in data given a suitable proxy for the cluster accretion rate.

Our analysis relies on a suite of hydrodynamical simulations from the Three Hundred Project. These are a set of re-simulations of 324 cluster-centred regions extracted from the MultiDark Planck 2 simulation (hereafter MDPL2). The Three Hundred Project provides a large number of massive clusters, while also providing high-resolution gas physics necessary to capture shocks.

The paper is organized as follows. In Section 2, we describe the Three Hundred Project simulations, how we extract Compton y maps from the simulations, and how we use these to construct mock-observed Compton y profiles. We present our analysis of these simulated profiles in Section 3 and conclude in Section 4.

2 SIMULATED DATA

2.1 The Three Hundred Project

The simulated galaxy clusters studied in this work belong to the Three Hundred Project, which is described in Cui et al. (2018). The sample consists 324 spherical regions centred on each of the most massive clusters identified at \(z = 0\) within the MDPL2 simulation (Klypin et al. 2016), a \((1 \, h^{-1}\, \text{Gpc})^3\) DM only simulation containing 3840\(^3\) DM particles and using Planck 2016 cosmological parameters (Planck Collaboration XIII 2016; \(\Omega_m = 0.307, \Omega_b = 0.048, \Omega_\Lambda = 0.693, \sigma_8 = 0.823, n_s = 0.96, h = 0.678\)). The clusters are initially selected according to their halo virial mass \(M_{\Delta_{200}} \approx 8 \times 10^{14} \, h^{-1} \, M_\odot\) at \(z = 0\). However, a much larger region (beyond the Lagrangian volume of the cluster) with radius \(R = 15 \, h^{-1} \, \text{Mpc}\) and centred on the minimum of the cluster potential at \(z = 0\) is used to generate the initial conditions for each cluster with multiple levels of mass refinement using the GINNUNGAGAP code; i.e. the particle number at the outer region is decreased based on their distance to the cluster centre to provide the gravitational field at the largest scales. These initial conditions are re-simulated with several variations using different baryon models and hydrodynamic solvers: GADGET-X (Murante et al. 2010; Rasia et al. 2015), GADGET-MUSIC (Sembolini et al. 2013), and Gizmo-SIMBA (Cui et al., in preparation). Given the large volume of the re-simulated regions (which exclusively include the cluster environment) and the multiple models employed to simulate the baryonic physics, these clusters have been used in several studies (see Wang et al. 2018; Arthur et al. 2019; Mostoghiu et al. 2019; Ansarifar et al. 2020; Haggard et al. 2020; Knebe et al. 2020; Kuchner et al. 2020; Li et al. 2020; Vega-Ferrero et al. 2021; Capalbo et al. 2021).

The analysis in this work is based on the GADGET-X model. It is a modified version of GADGET3 Tree-PM code and includes an improved SPH scheme with Wendland interpolating C4 kernel, and time-dependent artificial thermal diffusion and viscosity. Some other main features of this simulation are the gas cooling with metal contributions, star formation with chemical enrichment with AGB phase (Tornatore et al. 2007), supernovae and AGN feedback (Steinborn et al. 2015). The re-simulated clusters have a mass resolution (in the high-resolution region) of \(m_{\text{DM}} = 1.27 \times 10^7 \, h^{-1} \, M_\odot\) for the DM particles and \(m_{\text{SPH}} = 2.36 \times 10^8 \, h^{-1} \, M_\odot\) for the gas particles. We note that the stability of simulated cluster entropy profiles to the choice of numerical code has been studied by Sembolini et al. (2016).

2.2 y maps from the Three Hundred simulations

Compton y maps for each cluster are generated with the PYMSZ package, which has been presented in Cui et al. (2018) (see Baldi et al. 2018 for the kinetic SZ effect maps generated by this package). To generate the y maps, we use all the simulation data within a radius of 12 Mpc \(h^{-1}\) from the centre of the re-simulation region. The signal is smoothed into a 2D-mesh with size of 5 kpc using the same SPH kernel as the simulation. This pixel size corresponds to an angular resolution of 2.5316 arcsec, significantly higher resolution than the current and planned data sets that we consider. In this work, we mainly focus on Compton y maps generated from cluster snapshots a redshift of \(z = 0.193\). This choice is motivated by the fact that ongoing and future SZ surveys will detect many clusters near this redshift, and it is sufficiently low that narrow shock features are likely to be resolved by roughly 1 arcmin resolution experiments.

We note that the simulations used to generate the y maps do not treat the electron gas and ion gas separately, but rather consider both as a gas at a single temperature. When the gas density is high, the electrons and ions reach thermal equilibrium quickly, making this a good approximation. However, in the cluster outskirts relevant to this study, the gas density is low and the equilibration time can be large. Since the ions carry most of the kinetic energy of infall due to their larger mass, shock heating results in the ions reaching significantly higher temperatures than the electrons and maintaining this temperature difference for a significant period of time (Rudd & Nagai 2009). Since it is the electrons that are primarily responsible for the SZ effect, the different temperatures of the ions and electrons can in principle impact the observables considered in this work. Rudd & Nagai (2009) used simulations to investigate the impact of this effect on SZ observations, finding for relaxed clusters a roughly 10 per cent effect on the y profile near the shock radius. Since we focus on relaxed clusters, and since the errors on the y profiles in our analysis are significantly larger than 10 per cent near the shock radius (see e.g. Fig. 5), it is unlikely that this effect will significantly impact our main results. We postpone a more careful investigation of this effect to future work.

2.3 Cluster selection: identifying relaxed and not relaxed clusters

As we show below, relaxed clusters can provide a cleaner environment in which to look for shock features in the cluster y profiles than not relaxed clusters. Recent mergers and significant substructure
introduce features in the $y$ profiles that could interfere with our ability to identify features caused by shocks. For the most part, therefore, we will focus our analysis on a subset of clusters deemed to be relaxed. Since one of the main aims of this analysis is to determine the feasibility of detecting shock features in future data, we will adopt a relaxation criterion that can (at least approximately) be determined from data.

We use the $f_{\text{sub}}$ criterion (defined as the mass fraction in substructures identified within $R_{200}$ of the main halo) to determine the relaxation state of the clusters, as this quantity can be inferred from observations through (satellite) galaxy–halo relations. The halo and galaxy catalogue was identified with the AMIGA Halo Finder (Knollmann & Knebe 2009). The lowest mass structure has at least 32 particles (including DM, gas, and stars). Our ‘relaxed’ selection is

$$f_{\text{sub}} < 0.1,$$

which contains 68 clusters. We note here that $f_{\text{sub}}$ correlates with the centre of mass offset (Cui et al. 2017). Including centre of mass offset as an additional parameter to quantify the cluster dynamical state only results in a small change to the sample. As we discuss in more detail in Section 3.6, $f_{\text{sub}}$ correlates with the shock radius, as expected since higher $f_{\text{sub}}$ haloes will generally be faster accretors. The measured shock radius is therefore somewhat sensitive to our $f_{\text{sub}}$ selection. We also note that when stacking clusters, we throw out an additional six clusters for which $R_{200}$ is so large that we cannot reliably estimate the $y$ profile at large $R/R_{200}$, because of the restrictions imposed by the finite high-resolution regions of the simulation. The mean mass of the removed clusters is $\langle M_{200}\rangle = 1.27 \times 10^{15} \, M_\odot$.

2.4 Mock observations

Several observational effects are expected to degrade our ability to detect shock features around galaxy clusters with future SZ data sets. These include instrumental and foreground noise, the washing out of small-scale features by the telescope beam, and scatter in the mass-observable relations (which interferes with our ability to correctly scale the sizes of clusters when averaging their profiles). We will explore the consequences of these effects by adding them to simulated data.

We incorporate $y$ noise into the analysis by generating Gaussian noise realizations of the expected instrumental and foreground noise for observations by CMB-S4. The $y$ noise forecasts for CMB-S4 are taken from Abazajian et al. (2019).

The impact of the telescope beam is simulated by convolving the two-dimensional Compton $y$ images with a Gaussian beam. We assume $\sigma_{\text{beam}} = 1$ arcmin, corresponding roughly to the resolution of $y$ maps that will be produced by CMB-S4. As noted previously, all simulated clusters are at $z = 0.193$. Real clusters will of course be spread over some distribution in redshift, and will therefore experience different levels of beam smoothing in terms of physical scale. However, as long as the cluster sample is at $z \leq 1$, we do not expect a significant impact of the beam on the identification of shock features, as we show below.

When computing the averaged Compton $y$ profiles for the simulated clusters, we rescale each profile in the radial direction by the value of $R_{200}$ for each cluster (see discussion and motivation for using $R_{200}$ in Section 2.5). This scaling ensures that the shock features occur in roughly the same location for each cluster, and significantly enhances the signal to noise of the shock features in the average $y$ profile. However, for real data, the true cluster $R_{200}$ is unknown. Instead, we envision that a noisy estimate of the cluster mass will be used to form an estimate of $R_{200}$. We model the uncertainty in the cluster mass estimates by assigning each cluster an ‘observed’ mass drawn from a Gaussian centred on the true cluster mass, $M_{200}$ and with scatter $\sigma = 0.05 M_{200}$, fairly typical of the level of scatter expected for the SZ observable $Y_{\text{SZ}}$ (Green et al. 2020). These observed masses can then be used when estimating $R_{200}$ for the purposes of stacking.

2.5 Compton $y$ profiles

We compute the azimuthally averaged Compton $y$ profiles of all the simulated clusters. The profiles are first computed using 50 logarithmically spaced radial bins between 0.05 and 12 Mpc. These profiles are then interpolated on to logarithmically spaced bins of $R/R_{200}$. As discussed in Lau et al. (2015), the infall of gas on to a galaxy cluster after departure from the Hubble flow is determined by the enclosed mass at that time, which is set by the matter density. Since the outer gas profiles of low-redshift galaxy clusters are formed at late times during dark energy domination, the critical density of the Universe departs significantly from the matter density, and $\rho_m$ provides a better measure of the enclosed mass than $\rho_c$. Therefore, the outer profiles of clusters are more self-similar when scaled by $R_{200}$ rather than $R_{200}$. For the cases where we include observational scatter in the mass-observable relation, we use the mock-observed mass discussed above to compute $R_{200}$. Within each radial bin, we compute the average Compton $y$ value for the mock clusters to construct an azimuthally averaged $y$ profile. The cluster $y$ profiles are then averaged across various subsets of clusters, as we discuss below. The covariance of the average profile is computed using a leave-one-out jackknife.

In several cases, we find it useful to compute the logarithmic derivatives of the measured Compton $y$ profiles. To do so, we follow the procedure introduced in Diemer & Kravtsov (2014). For each cluster, we smooth its logarithmic $y$ profile using a Savitsky–Goaly filter of window size 5 and polynomial order 2. The smoothed profile is then fit with a cubic spline, evaluated on a very fine radial grid, and the derivative is computed with finite differences. We find that our results are not very sensitive to the window size or polynomial order of the Savitsky–Goaly filter, provided these are not chosen to introduce so much smoothing that the profile features are washed out.

3 RESULTS

3.1 The Compton $y$ profiles of individual clusters

We first consider the Compton $y$ profiles of individual clusters, arguing that features due to external shocks can be seen in these profiles. However, we will show that detecting these features in data from future SZ surveys will require averaging across clusters to increase the signal to noise, motivating the subsequent analysis discussed in Section 3.2. Fig. 1 shows example Compton $y$ maps for an unrelaxed (left) and relaxed (right) cluster; the determination of relaxation state is described in Section 2.3. The clusters have close to the same mass, $M_{200} \approx 1.45 \times 10^{15} h^{-1} M_\odot$. The central crosshairs indicates the location of the halo centre as determined...
from the maximum density peak in AHF. The not relaxed cluster has a less circular and less extended $y$ signal, shows an indication of substructures, and exhibits a larger contribution from nearby filaments. The blue circle in each panel indicates $R_{200m}$ for the clusters. We will return to the other coloured circles below.

Fig. 2 shows a sample of the cluster $y$ profiles (top panels) for some of the not relaxed (left) and relaxed (right) clusters in the full sample. The black lines indicate the profiles for the two clusters seen in Fig. 1. We have normalized the radial coordinates relative to the $R_{200m}$ of each cluster, as discussed in Section 2.5. There is clearly large scatter between the profiles, as the clusters have different masses and different levels of nearby structure. The not relaxed clusters typically exhibit more scatter and more fluctuations in their $y$ profiles owing to the presence of large nearby haloes.

Gas within the external shock boundary has significantly higher pressure than gas outside the shock. Consequently, such shocks are associated with a sudden decline in the cluster pressure profile as one moves away from the cluster centre. This decline is often preceded by a flattening of the pressure profile, as one nears the recently shocked gas (Molnar et al. 2009). Since $y$ is proportional to the line-of-sight integral of the pressure profile, we expect shocks to lead to similar behaviour in the $y$ profile, albeit smoothed out by the line-of-sight integration. Indeed, in several of the profiles of the relaxed clusters shown in Fig. 2, there is an apparent flattening of the profile, followed by a subsequent steepening at roughly $2R_{200m}$. This feature is especially clear for the relaxed cluster from Fig. 1 (shown with the black curves in the right-hand panels of Fig. 2), but can be easily seen for the other relaxed clusters, and some of the not relaxed clusters, as well. These features, and their location at roughly $2R_{200m}$, are consistent with the shock features identified in the analysis of Molnar et al. (2009). There is also a weaker minimum in the logarithmic derivative of several clusters near $R_{200m}$.

In order to more clearly see the flattening and subsequent steepening of the Compton $y$ profile that is associated with shocks, we take the logarithmic derivatives of the $y$ profiles using the procedure described in Section 2.5; these are shown in the bottom panels of Fig. 2. The logarithmic derivative profiles for several clusters exhibit minima near to $2R_{200m}$. We note that some of the relaxed and not relaxed clusters exhibit minima in their logarithmic derivative profiles at multiple radii. This is not surprising: clusters can have multiple shocks, and some features in the $y$ profiles may not be due to shocks at all, but rather to variations in the gas density around the clusters. The orange rings in Fig. 1 indicate the locations of minima in the logarithmic derivative profiles of the clusters.

Fig. 2 also shows the noise level projected for $y$ profile measurements with CMB-S4 (dotted black line). This noise curve represents the standard deviation of the profile from noise alone, where the noise is calculated using Gaussian realization of the $y$ noise power spectrum described in Section 2. Note that the noise profile is sensitive to the radial binning: finer bins will have higher noise variance as they average over a smaller area of sky. For the purposes of this plot, we adopt 10 bins between 0.1 and $4R_{200m}$. It is clear from Fig. 2 that it will be difficult to directly measure shock features around individual clusters in data from CMB-S4: the standard deviation of the noise is larger than the amplitude of the $y$ profile at $2R_{200m}$, where the shocks features occur. This motivates our decision to focus on the Compton $y$ profiles averaged over many galaxy clusters. However, detection of shock features in the $y$ profiles of individual clusters may still be possible, particularly for features at lower radial distances (such as virial shocks) and for very massive clusters. Indeed Hurier et al. (2019) have recently claimed a detection of a virial shock around a massive cluster using Planck $y$ maps.

In addition to measuring the cluster $y$ profiles at fixed redshift, it is also useful to consider the evolution of the logarithmic derivative profiles as a function of redshift. Taking as an example the relaxed cluster shown in the right panel of Fig. 1, Fig. 3 shows the evolution of the logarithmic derivative of this cluster’s $y$ profile over the range of $0.1 < z < 0.3$. Although nearby matter (haloes and gas) is infalling into the cluster, the evolution of the logarithmic derivative minimum is a movement outward. This is consistent with the association of the minimum in the logarithmic derivative with cluster shock features, since the shock boundary is expected to grow as the cluster accumulates more gas.
Figure 2. Example Compton $y$ profiles of not relaxed (left) and relaxed (right) clusters. Top panels show the Compton $y$ profiles, while the bottom panels show the logarithmic derivatives of this quantity. Steepening of the $y$ profiles of the relaxed clusters at roughly $2R_{200}$ is evident for many of the clusters. The black lines correspond to the profiles of the two clusters shown in Fig. 1.

Figure 3. Evolution of the logarithmic derivative of the Compton $y$ profile. The profiles shown correspond to the relaxed cluster in Fig. 1.

We next consider the distribution of minima in the logarithmic derivatives of the $y$ profiles of all the simulated clusters. Fig. 4 shows this distribution, split on the depth of the minima in the logarithmic derivative. Note that a single cluster can have multiple minima that appear in this figure. The deep minima with slopes less than $-6$ group together around $2R_{200}$, which we associate with the external shocks. The clusters also show a preference for shallow minima at roughly $R_{200}$, which may be due to so-called virial shocks (Molnar et al. 2009).

While minima in the logarithmic derivative profiles are (at least sometimes) associated with shocks, we emphasize that the locations of these minima do not necessarily coincide exactly with the locations of shocks identified from the peaks of the entropy profile (e.g. as in Lau et al. 2015). For one, $y$ is a projected quantity while the peak of the entropy profile is measured in 3D. This means that the $y$ profile, unlike the 3D entropy profile, can be significantly impacted by line-of-sight projections of nearby structure. Furthermore, as seen in Molnar et al. (2009), even in 3D, the entropy profile does not peak exactly at the location of the steepest slope of the pressure profile. None the less, as we show in Section 3.4, it appears that the location of the minimum in the logarithmic derivative of the cluster-averaged $y$ profile agrees well (to tens of percent in radius) with the location...
of the maximum (in absolute value) of the cluster-averaged gas infall velocity, i.e. where the external shock is expected. This suggests that when averaging over many clusters, the projected radius of the minimum in the logarithmic derivative of \( y \) is in rough agreement with the 3D radius of the external shock.

### 3.2 The stacked Compton \( y \) profiles

Motivated by the discussion above, we now explore the possibility of averaging \( y \) profiles from multiple clusters to improve the signal to noise of external shock measurements. It is not obvious that averaging the \( y \) profiles of multiple clusters is a sensible way to improve the signal to noise of shock measurements. As seen in Fig. 2, there is considerable scatter in the \( y \) profiles of clusters, and this scatter could cause the shock features to disappear in the stack. However, we will show below that as long as the profiles are rescaled by \( R_{200m} \), a clear feature emerges in the stacked Compton \( y \) profiles that is associated with external shocks.

The top panel of Fig. 5 shows the uncertainty band on the average Compton \( y \) profile of the relaxed sample of clusters, computed as described in Section 2.5. The profile exhibits a flattening, followed by a rapid steepening at roughly \( 2R_{200m} \). The minima tend to occur at roughly \( R_{200m} \) and \( 2R_{200m} \). The minima near \( 2R_{200m} \) are typically deeper (corresponding to more negative logarithmic slopes) than those near \( R_{200m} \).

There is a deep minimum in the logarithmic derivative near \( R_{200m} \), which we associate with external shocks in the individual cluster \( y \) profiles. The orange curve represents the sum of the one- and two-halo terms. The stacked cluster profile exhibits a plateau at \( R/R_{200m} \sim 2 \), followed by a rapid decline. We associate this feature with outer shocks in the individual cluster \( y \) profiles. The top panel of Fig. 5 shows the uncertainty band on the average Compton \( y \) profile of the relaxed sample of clusters, computed as described in Section 2.5. The profile exhibits a flattening, followed by a rapid steepening at roughly \( 2R_{200m} \). The minima tend to occur at roughly \( R_{200m} \) and \( 2R_{200m} \). The minima near \( 2R_{200m} \) are typically deeper (corresponding to more negative logarithmic slopes) than those near \( R_{200m} \).

The bottom panel of Fig. 5 shows the logarithmic derivative of the stacked Compton \( y \) profile when the cluster sample is restricted to those clusters that do not have massive nearby neighbours.

The green dotted curve in the top panel of Fig. 5 shows the expected \( y \) profile derived from the Battaglia et al. (2012) pressure profile. The Battaglia et al. (2012) profile was derived from fitting the inner part of the cluster pressure profiles in hydrodynamical simulations, so it is not surprising that it agrees with our results very well at small scales. At large scales, however, the profile departs from the measurements as a result of the shock feature, and the contributions from nearby haloes, which we discuss in more detail below.

#### 3.3 The impact of nearby haloes on the \( y \) profile

One might worry that the presence of nearby haloes could impact our ability to detect features associated with external shocks in the cluster-averaged Compton \( y \) profile. As shown in Power et al. (2020), massive infalling substructures can produce clear signatures of shocks in the direction of their motions. Furthermore, overdensities of gas in nearby haloes could produce features in the \( y \) profile that
appear similar to the features caused by shocks. We will argue below that while nearby haloes do have an impact on the Compton $y$ profiles of clusters, they do not significantly impact our main conclusions about the shock features in the average $y$ profile of many clusters.

In the language of the halo model (Cooray & Sheth 2002), the contributions to the cluster-centric $y$ profile coming from nearby haloes is the two-halo term. The two-halo term in the context of the halo–$y$ correlation has been considered by several authors (e.g. Komatsu & Seljak 2002; Vikram, Lidz & Jain 2017). The expected two-halo term for the clusters in the sample is shown as the purple dashed curve in the top panel of Fig. 5. We compute the two-halo term as described in Pandey et al. (2019), adopting the Battaglia et al. (2012) pressure profile model and a linear bias model to describe halo clustering. The two-halo term offers a reasonable description of the $y$ profile at large $R/R_{200m}$, despite simplifications such as our assumption of linear bias. The total halo model profile is the sum of the one- and two-halo terms, shown as the orange curve in the top and bottom panels of Fig. 5. While the shock feature in the cluster-averaged $y$ profile occurs near to the one-to-two halo transition, it appears qualitatively different from the halo model prediction for this transition. The shock feature results in a plateauing of the $y$ profile, followed by a steep decline, followed by the resumption of a less steep profile (top panel of Fig. 5). The one-to-two halo transition, however, does not exhibit any such steep decline. The bottom panel of Fig. 5 shows that the logarithmic derivative of the total halo model prediction never goes below $-3$, while the logarithmic derivative of the simulated cluster profiles reaches slopes as steep as $-5$ and steeper. In other words, assuming the cluster pressure profile of Battaglia et al. (2012), the halo model fails to provide an accurate description of shock features in the Compton $y$ profile. This is not surprising, as the halo model prediction includes no information about the shocking of gas.

To test the impact of large nearby haloes on the inferred shock locations, we repeat our analysis after removing any of the clusters that have a neighbour with $M > 8 \times 10^{13} M_\odot$ within 10 Mpc. This selection reduces the number of relaxed clusters to 13. A comparison between our results with all relaxed clusters and the results found when additionally excluding clusters with massive neighbours is shown in the bottom panel of Fig. 5. Since the exclusion criterion significantly changes the cluster sample, we do not expect the $y$ profile to remain unchanged. Indeed, selecting haloes without nearby massive neighbours amounts to a selection on cluster environment, which correlates strongly with accretion rate. We expect then, that this selection may modify the shock location to some extent (see further discussion of this point in Section 3.6). None the less, Fig. 5 shows that the appearance of the shock feature is fairly robust to the selection of clusters without massive neighbours. In principle, one could also attempt to remove two-halo contributions to the cluster-$y$ profile by selecting isolated clusters; however, see Hill et al. (2018) for an explanation of why this approach presents additional difficulties.

3.4 Connecting the $y$ profile with other halo properties

Accreting gas rapidly decelerates and increases in temperature as it passes through the external shock. Consequently, we expect the shock features observed in the $y$ profile to be related to features in the gas velocity and temperature profiles. Fig. 6 explores these connections.

The top panel of Fig. 6 shows the logarithmic derivative of the cluster-averaged $y$ profile, as in Fig. 5. For this figure, we consider only the relaxed sample of clusters. The middle panel of Fig. 6 shows the average radial velocity profile of the gas for the same set of clusters. The narrow minimum in logarithmic derivative of Compton $y$ closely corresponds with the minimum in the radial velocity profile. This supports our interpretation of the feature in the averaged $y$ profile as being due to the outer shock. Note we use two different radii in Fig. 6: the $y$ profile is a projected quantity and we therefore plot it as a function of the projected radial distance, $R$, while the radial velocity profile and temperature profiles are measured as functions of the three-dimensional radial distance, $r$.

The bottom panel of Fig. 6 shows the logarithmic derivative of the averaged cluster temperature profile. As one moves to larger radius near the shock location, the temperature profile becomes steeper and steeper. This is expected, as the temperature of the gas increases as it passes through the shock.

3.5 Impact of observational uncertainties

We now consider how three observational effects can impact our results: (1) the instrumental beam, (2) noise in the Compton $y$ maps, (3) uncertainty on the value of $R_{200m}$ used when rescaling the profiles.
3.6 Splashback and shocks: correlation between the splashback radius and shock location

Recently, the splashback radius has been established as the boundary of the virialized, or multistreaming region of the DM component of a halo (Adhikari et al. 2014; Diemer & Kravtsov 2014). This surface traces the boundary of the first apocentre of the most recently accreted material, separating a region of DM infall from the regions within which DM particles or other collisionless objects like galaxies orbit. Arguably, the external shock forms the boundary of the gaseous component of the halo.

It is known that both the locations of external shocks and the locations of the outer caustic in the DM distribution both depend on the evolution history of the halo (Bertschinger 1985; Shi 2016). In particular, both these features are a function of the mass accretion rate of the halo. We therefore expect the splashback radius and the shock location to be correlated. Although analytical studies with self-similar models (Bertschinger 1985) showed that the location of the accretion shock coincides with the location of the outer caustic, studies in simulations have shown that external shocks can exist far outside the virial boundary of the halo (Molnar et al. 2009; Zhang et al. 2019; Zhang et al. 2020). In this section we investigate how the shock features in the averaged Compton y profiles correlate with the splashback feature in the DM profiles of clusters.

While the actual splashback surface is ideally measured from the apocentre of particle orbits as in Diemer (2017), we measure the splashback radius here as the location of the minimum of the slope in the logarithmic density profile. This radius is known to capture the phase space transition between the infall and virialized region and is moreover accessible observationally (e.g. More et al. 2015).

We compare the shock and splashback radii for clusters as a function of the accretion history of the halo. We use $f_{\text{sub}}$, the mass fraction of the cluster in substructure, as a proxy for the accretion rate. This quantity is potentially observable and is related to the number of bright satellites in clusters. Young haloes that have large satellite fractions. With time, as the halo stops growing and enters a slow accretion phase, substructure gets destroyed due to tidal effects and dynamical friction. $f_{\text{sub}}$ is therefore strongly correlated to the accretion rate of the cluster as shown in the left-hand panel of Fig. 8. The accretion rate of the cluster, $\Gamma = d\log M_{200}/d\log a$, is obtained from the mass accretion history measured from the simulation. We evaluate the slope of the mass history at $z=0.193$ by fitting the function $M\propto e^{-a/c}$ (Wechsler et al. 2002) to the mass between the 0.193 < $z$ < 0.350.

In order to explore the relation between shock and splashback radius, we divide the cluster sample into two subsets with different $f_{\text{sub}}$. We first remove clusters with $\Gamma > 4$ (the grey region of the left-hand panel of Fig. 8), as clusters with large $\Gamma$ may be in the process of major mergers. We then split the remaining cluster sample in halves based on the median value of $f_{\text{sub}}$. The value of $f_{\text{sub}}$ used for this split is shown as the horizontal dashed line in the left-hand panel of Fig. 8.

In the right-hand panel of Fig. 8, we show the relation between the location of the shock and the location of the splashback radius for the two cluster subsamples split on $f_{\text{sub}}$. The shock radius is determined from the location of the minimum of the logarithmic derivative of the averaged y profile, while the splashback radius is determined from the averaged subhalo density profiles. Both radii are normalized by $R_{200\text{sub}}$, so any correlation between the cluster mass and the two radii is effectively cancelled. We see that haloes with high $f_{\text{sub}}$, corresponding to high accretion rate, have both a smaller splashback radius and a smaller shock radius. The dependence of the splashback radius on accretion rate is expected, as particle apocentres become smaller due to the rapid growth of the halo potential (Diemer & Kravtsov 2014). We see a similar behaviour in the location of the outer shock. The correlations between splashback and shock radius has previously been seen in simulations (Walker et al. 2019; Aung et al. 2021). Our result here shows that this correlation persists when the shock...
Fig. 8. Left: The quantity $f_{\text{sub}}$ that we use to identify the relaxed population of clusters is correlated with the cluster accretion rate, $\Gamma$, with correlation coefficient of $r = 0.6$. The grey band illustrates our cut on cluster accretion rate imposed when computing the measurements shown in the right-hand panel. The dashed horizontal line indicates the median $f_{\text{sub}}$ of the remaining clusters, which is used to split the full sample into the high and low $f_{\text{sub}}$ subsamples shown at right. Right: The shock radius and splashback radius are correlated. The shock radius here is identified using the minimum of the logarithmic derivative of the cluster-averaged $y$ profile, while the splashback radius is identified from the DM particles as described in the main text. The two data points shown correspond to the cluster samples defined in the left-hand panel.

location is estimated from the minimum of the logarithmic derivative of the stacked $y$ profile.

Fig. 8 also makes it clear that the inferred shock location will vary depending on the $f_{\text{sub}}$ cuts. Our nominal cut of $f_{\text{sub}} < 0.1$ corresponds (very) roughly to the blue point in the right-hand panel of Fig. 8. As we consider clusters with higher $f_{\text{sub}}$, the shock location decreases, and the profiles exhibit more scatter, as seen in Fig. 2. As a result the errorbars on the shock position for the high $f_{\text{sub}}$ sample are larger than those for the low $f_{\text{sub}}$ sample. An analysis in data would need to consider the signal-to-noise trade off between increasing the number of clusters and increasing the scatter in individual cluster $y$ profiles as the $f_{\text{sub}}$ (or other accretion rate proxy) cut is relaxed.

4 DISCUSSION

4.1 Summary

The outskirts of galaxy clusters reflect their recent accretion history and their local environments. The collisional gas accreting on to clusters experiences shocks at several $R_{200m}$ that significantly impact the thermodynamic properties of the ICM. We have presented an exploration of the detectability of shock features in the stacked Compton $y$ profiles of massive galaxy clusters. Because DM is collisionless, on the other hand, its accretion gives rise to the splashback boundary of the cluster, and a corresponding feature in the cluster mass profile. We have explored the correlation between shock features in the cluster $y$ profiles and the splashback features in the cluster mass profiles.

Gas shocks in cluster outskirts have proven difficult to constrain observationally because of the low gas densities in the cluster outskirts. One promising route to detection is via the SZ effect. However, current and future wide-field SZ surveys are unlikely to have the sensitivity to detect these features around individual clusters (except perhaps the most massive ones), as we have shown. Motivated by these considerations, we show that stacking cluster $y$ profiles as a function of $R/R_{200m}$ can provide a promising route to constraining shock features around future samples of galaxy clusters. We demonstrate that outer shocks result in a narrow minimum in the logarithmic derivative of the stacked cluster $y$ profile. This shock-associated feature is robust to smoothing by instrumental beams and uncertainty in $R_{200m}$. Furthermore, for realistic levels of noise (i.e. typical of CMB-S4), high significance detections of the shock features can be obtained with samples of roughly a thousand clusters. Such detections may already be in reach of ongoing CMB surveys such as SPT-3G and AdvACT.

4.2 Implications

We have shown that shock features are detectable in the averaged $y$ profiles of galaxy clusters with near-term CMB data. Obtaining such a detection is an exciting prospect. The locations and properties of shocks are connected to the cluster accretion rate and the cluster’s large-scale environment. Measurement of the shock radius in the averaged $y$ profile could be used to test different proxies for the accretion rate, and to compare to simulations. Detection of shocks using SZ observations in conjunction with measurements of the cluster splashback radius using weak lensing (e.g. Chang et al. 2018) will provide insight into cluster outskirts in gas and total mass. Detection of cluster external shocks in large cluster samples may also enable improved constraints on models of cosmic ray acceleration in the shock fronts. Moreover, the statistical detection of shocks explored here can open up a new window into studying how the properties of galaxies change as they cross the shock and splashback boundaries of clusters (e.g. Baxter et al. 2017; Shin et al. 2019; Adhikari et al. 2020).

However, the detection of shock features also poses some challenges. In particular, if these features can be detected at high significance, modelling these features may be necessary for analysing high-precision observables derived from the SZ effect. In particular, current analyses of the SZ power spectrum and cross-correlations with the SZ typically do not include shock features when modelling these observables. Working in physical coordinates (rather than coordinates rescaled by $R_{200m}$) will smear out the shock features, but some impact from the shocks may remain. We postpone a more careful investigation of the effects of shocks on other observables to future work.
ACKNOWLEDGEMENTS

We thank Dhayaa Anbajagane, Neal Dalal, Andrey Kravtsov, Shivam Pandey, Debora Sijacki, and Congyao Zhang for useful discussions related to this paper. WC acknowledges support from the European Research Council under grant number 670193 and further acknowledges the science research grants from the China Manned Space Project with No. CMS-CSST-2021-A01 and CMS-CSST-2021-B01. AK is supported by the Ministerio de Ciencia, Innovación y Universidades (MICIU/FEDER) under research grant PGC2018-094975-C21 and further thanks Cocteau Twins for victorialand.

DATA AVAILABILITY

The data used to generate the figures in this work are available upon request.

REFERENCES

Li Q. et al., 2020, MNRAS, 495, 2930  
Pandey S. et al., 2019, Phys. Rev. D, 100, 063519  

This paper has been typeset from a TeX/LaTeX file prepared by the author.