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# Aggregating value systems for decision support

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## ABSTRACT

We adopt an emerging and prominent vision of human-centred Artificial Intelligence that requires building trustworthy intelligent systems. Such systems should be capable of dealing with the challenges of an interconnected, globalised world by handling plurality and by abiding by human values. Within this vision, pluralistic value alignment is a core problem for AI– that is, the challenge of creating AI systems that align with a set of diverse individual value systems. So far, most literature on value alignment has considered alignment to a single value system. To address this research gap, we propose a novel method for estimating and aggregating multiple individual value systems. We rely on recent results in the social choice literature and formalise the value system aggregation problem as an optimisation problem. We then cast this problem as an  $\ell_p$ -regression problem. Doing so provides a principled and general theoretical framework to model and solve the aggregation problem. Our aggregation method allows us to consider a range of *ethical principles*, from utilitarian (maximum tility) to egalitarian (maximum fairness). We illustrate the aggregation process and the European Values Study. Our experimental evaluation shows how different consensus value systems can be obtained depending on the ethical principle of choice, leading to practical insights for a decision-maker on how to perform value system aggregation.

## 1. Introduction

The vision of human-centred Artificial Intelligence (AI) has spurred research on trustworthy, ethical AI that enhances human capabilities and empowers citizens and society to deal with the globalised world's challenges effectively. Thus, developing trustworthy AI [1] that abides by human values is a primary AI concern, as explicitly stated by the European Commission's Ethics Guidelines for Trustworthy AI [2], the Artificial Intelligence Act [3], and the IEEE's Global Initiative on Ethics of Autonomous and Intelligent Systems [4]. Within this vision, a core problem is AI value alignment, which aims to ensure that AI is properly aligned with human values [5]. Designing an AI agent to align with human values means that the agent does "what it morally ought to do, as defined by the individual or society"<sup>1</sup> [6].

The problem of value alignment has spurred research on different aspects of the challenge such as formalising the value alignment problem [7], identifying relevant values [8], value-sensitive design [9–11],

learning value-aligned behaviours [12–18], reasoning about values to act ethically [19–21], and aligning norms with values [22–24]. A core component of the different value alignment endeavours is the concept of a *value system*, which models how an entity (e.g., an individual or an organisation) interprets and prioritises values. A common assumption in most state-of-the-art research on value alignment is that an AI system must align with *one* value system, be it that of an individual or a society. However, as Gabriel [6] argues, by following Rawls, humans may hold various reasonable but contrasting beliefs about values. That is, we live in a pluralistic world where people hold different value systems. Designing an AI system that aligns with a group of people with different value systems poses the *pluralistic value alignment* problem [6]. This is the case, for instance, when making policy decisions that align with stakeholders having a variety of value systems (e.g., when deciding over water governance [25,26]) or when designing human-agent teams

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<sup>&</sup>lt;sup>1</sup> Therefore, hereafter we shall refer to human values as moral values, or simply as values for shorter when there is no risk to incur in confusion.

involving humans with differing ethical perspectives (the most apparent examples exist in the medical field, where teams are constantly tasked with scenarios that require ethical consideration) [27].

In this paper, we address the following research question: how to determine the value system(s) that an AI system should align with, considering value diversity? More precisely, we make headway in the pluralistic value alignment problem by addressing the aggregation of different value systems to yield a *consensus* value system. We assume that the value systems to aggregate belong to any form of individual entities, be they citizens, stakeholders, teammates, countries, or even supra-national entities. To succeed in this endeavour, we identify three major challenges.

First, as noted by Mittelstadt [28], existing ethical codes are rather abstract about moral values, hence not specific enough to guide actions. This is also typically the case in the AI literature on value systems (e.g., [23,29–31]). Therefore, it is necessary to precisely identify the key elements that a value system must include. Importantly, this effort must consider that: (i) value systems are *contextual* [8,32–34], i.e., the way in which we reason about and prioritise values is influenced by contextual factors such as actors and actions [35–37]; and (ii) individuals may ascribe different *interpretations* to the same value system [38]. Second, we need to *estimate* or characterise the value system of each individual [39]. Third, from a social choice perspective, value systems can be aggregated following different *ethical principles* (e.g., utilitarian or egalitarian). Therefore, we need a principled and general aggregation method that allows us to set the ethical principle of choice.

We approach the challenge of pluralistic value alignment by studying two real-world cases. On the one hand, we consider the data from a Participatory Value Evaluation (PVE) [40] process conducted in 2020 to gauge the opinion of the residents of a municipality in the Netherlands over energy policies [41]. From this data, we estimate the value system of each citizen who participated in the PVE. On the other hand, we consider data from the European Values Study (EVS) [42], an extensive survey conducted on European citizens to characterise the value systems of European countries.

We build on preliminary works on value aggregation [38] and value estimation [43] to make the following novel contributions:

- We extend the definition of value system to account for *contextuality* and *pluralism*. We show how the novel definition can be employed to represent individual value systems in the two case studies that we analyse.
- Based on the social choice (distance) functions from González-Pachón and Romero [44], we formalise the problem of aggregating different value systems following a given ethical principle (e.g., utilitarian or egalitarian), and we cast it as a two-step optimisation problem to obtain: (i) the aggregation of value interpretations from individuals, and (ii) the aggregation of the preferences of individuals over moral values.
- We show that the problem of computing the consensus value system can be cast as an  $\ell_p$ -regression problem [45] (also called norm approximation problem [46]). By doing so, we provide a general theoretical framework that allows us to solve the above-mentioned problem for a range of ethical principles from utilitarian (maximum utility) to egalitarian (maximum fairness) in a scalable and reliable way, thanks to recent results in the machine learning literature [45].
- We illustrate our value aggregation approach with real-world data from the PVE [41] and the EVS [42]. We conduct a thorough empirical evaluation that : (i) shows the impact of choosing different ethical principles on the resulting consensus value system; (ii) characterises the space of ethical principles to determine whether a given ethical principle produces a consensus leaning towards the utilitarian or the egalitarian ethical principle; and (iii) quantifies the price to pay when moving away from the

majority to include the minority. The aggregation results differ in the two case studies since they handle different data. However, we delineate the common trends we observe. Finally, we provide practical insights for decision-makers concerned with obtaining a consensus on different value systems according to an ethical principle of choice.

In summary, we provide both the computational means and the guidelines for a decision-maker to conduct the principled aggregation of value systems.

*Organisation.* Section 2 provides background on the distance functions that we require from the social choice literature. Section 3 identifies the key elements of a value system and introduces the value systems in our two case studies. Section 4 formalises our aggregation problem and Section 5 shows that it can be cast as an  $\ell_p$ -regression problem that can be solved as described in Section 5.1. Section 6 reports on our empirical findings and provides guidelines for the decision-makers in charge of the value system aggregation. Finally, Section 7 draws conclusions and sets paths to future research.

#### 2. Preliminaries: Distance functions

As mentioned above, the main goal of this paper is to aggregate the values and preferences on values (i.e., the value systems) of different individuals to yield a consensus value system. The basic problem in designing socially optimal decisions is aggregating individual preferences on multiple alternatives into a collective preference representing a consensus. This problem is the core of disciplines such as social choice (e.g., [47,48]), multi-expert decision-making (e.g., [49,50]), or group decision-making (e.g., [51-54]). Therefore, many procedures for undertaking this aggregation task have been proposed in the literature. However, methods for aggregating preferences holding "good" theoretical properties are needed to facilitate the acceptance of the resulting consensus by the group of individuals involved in the decision [44]. Designing aggregation functions that exhibit good social choice properties (e.g., unanimity, anonymity, non-dictatorship) is a major goal in the social choice literature [47]. For this reason, to tackle the aggregation problem that we pose in this paper, we resort to the tools in the social choice literature.

This section provides a background on the social choice functions that we employ. We borrow from existing work [44,55-57], which define a generator of social choice functions (as a *p*-parameterised distance function) to obtain a consensus in a society of individuals. The choice of this generator of social choice functions is motivated by several reasons. First, it is well-founded on the social choice literature and multi-criteria decision-making literature, following earlier work by Cook [58-61] and Yu's p-metric distance [62,63] respectively. Second, the literature (e.g., [55,64]) has already studied the social choice properties underlying the compromise consensuses derived from the selected social choice function (e.g., neutrality, monotonicity, anonymity). Third, the work in [56] shows that our social choice function allows us to solve a wide range of aggregation situations (involving both ordinal and cardinal preferences of individuals). Finally, the works in [44,55] offer interpretations of the consensus that the social choice function produces. This includes a study (limited to the cases of p = 1 and  $p = \infty$ ) of the *ethical* interpretation of the resulting consensus within a context of social choice. This means that our generator produces social functions that vary depending on ethical principles (e.g., egalitarian, utilitarian, equity).<sup>2</sup> Such ethical interpretations provide us with foundations to analyse consensuses.

 $<sup>^2\,</sup>$  In this paper, we do not consider the consensus computed considering the principle of equity (i.e., the so-called Marxian solution) since, as noted by the authors of [44], it often results in an over-constrained optimisation problem that yields no solution.

Thus, one of the major benefits of our generator of social choice functions is that it allows decision-makers to compute a consensus following different *ethical principles* according to different values of the parameterised distance function.

The general setting of González-Pachón and Romero [55] considers a society of *n* members (i = 1, ..., n). Each member of the society provides judgement on *m* objects (j = 1, ..., m), which can be candidates, criteria, alternatives, etc. In the case of aggregating value systems, the objects represent moral values. As argued in Section 3, rankings are typically used to describe value systems. Thus, we consider that each member of the society ranks their moral value preferences. Furthermore:

- $w_i$  is the weight (social influence) of the *i*th member.
- *R<sub>i</sub>[j]* is the rank position provided by the *i*th member of the society for the *j*th object (in our case, with the *j*th value) within the ranking.
- $R_S[j]$  is the *consensus* position assigned by the society as a whole to the *j*th object (in our case, with the *j*th value).  $R_S$  is the unknown consensus ranking that we seek to obtain.
- *p* is a metric parameter (i.e., an integer  $\geq$  1) that determines the *ethical principle* used to compute the consensus, in accordance with the terminology established in the social choice literature [44,55–57].

From the previous definitions, a generator of social choice functions based on the weighted Minkowski *p*-metric distance function  $(U_p)$  is introduced and described in several works [44,55–57] as:

$$U_p = \left[\sum_{i=1}^n \sum_{j=1}^m w_i |R_i[j] - R_S[j]|^p\right]^{1/p}.$$
 (1)

Given the distance function  $U_p$  and a value of p, the goal is to find the *consensus* values of  $R_S[j]$  that minimise the deviation between the judgements provided by the members of the society (data of the problem) and the consensus (the unknown).

In addition, González-Pachón and Romero [44] modify Eq. (1) to aggregate more complex objects besides rankings. In this case, they propose a distance function to aggregate a 2-dimensional vector such that

$$U_{p} = \left[\sum_{i=1}^{n}\sum_{j=1}^{m}\sum_{k=1,k\neq j}^{m}w_{i}|R_{i}[j,k] - R_{S}[j,k]|^{p}\right]^{1/p},$$
(2)

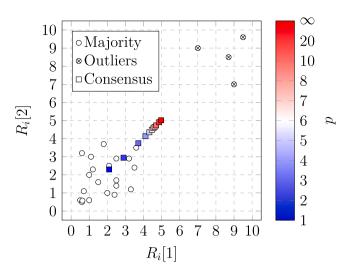
where  $R_i[j, k]$  is the judgement value provided by the *i*th member of the society when comparing the *j*th and the *k*th object. It is relevant that González-Pachón and Romero [56] shows how the social choice function in Eq. (2) can handle a wide range of aggregation situations. This includes aggregations when information about preferences is: ordinal and complete (complete rankings); ordinal and partial (partial rankings) ; and cardinal and complete (pairwise comparisons). Thus, when using Boolean values in the preference (*R*) matrix, we can express ordinal and qualitative preferences, whereas we can also express graded quantitative preferences through cardinal values. Furthermore, as argued in [44], the information in the preference matrix can be complete or incomplete.

From the  $U_p$  distance function, González-Pachón and Romero [44] derive two cases of interest. First, by setting p = 1, the general distance in Eq. (1) yields

$$U_B = \left[\sum_{i=1}^n \sum_{j=1}^m w_i |R_i[j] - R_S[j]|\right].$$
 (3)

The consensus that minimises  $U_B$  provides the social optimum from the point of view of the majority, i.e., the *utilitarian* solution (or Benthamite solution [65]) that maximises the total welfare.

By setting  $p = \infty$ , the distance function in Eq. (1) yields



**Fig. 1.** The impact of the ethical principle p on the computed consensus of a set of individuals' judgement of two objects:  $R_i[1]$  and  $R_i[2]$ . Circles show the individuals' judgement and squares represent the consensus computed. Squares are filled with the colour of the ethical principle used to compute the consensus.

Eq. (4) represents the Chebyshev distance, which is equivalent to the weighted Minkowski distance for  $p = \infty$ . In this case, finding the consensus implies minimising the disagreement of the member of the society most displaced with respect to the majority solution defined by the utilitarian case above (Eq. (3)). This solution is *egalitarian* [66] since it represents the social optimum from the point of view of the minority (from the perspective of the worst-off member of the society according to the Rawls' principle [67]), leading to the point of maximum fairness. Note that, when considering the limit case  $p \rightarrow \infty$ , the weighting scheme in Eq. (1) vanishes, hence the weight  $w_i$  does not appear in Eq. (4).

In addition to the utilitarian and egalitarian cases, we can use  $p \in [2..\infty)$  for computing different consensus. To illustrate the semantics of the ethical principle p and its impact on the consensus, we show a test case (with fabricated data) in Fig. 1, which plots the judgements of 25 individuals on two objects. The circles represent the individuals' judgements  $R_i[1]$  and  $R_i[2]$  about objects 1 and 2 within the x and y axis, respectively.

We clearly distinguish two groups of individuals: (1) a clustered set of individuals that represent the majority with values for *x* and *y* smaller than 4, and (2) a few individuals representing outliers distant from the majority (each shown in a crossed circle). In addition, the squares represent the position of the computed judgement consensus with different ethical principles, *p*'s, whose values are represented with a colour scale from blue (p = 1) to red ( $p = \infty$ ). As we can observe, the utilitarian consensus (p = 1) is at the centre of the majority. As we increase *p*, the consensus moves towards the outliers, converging to the egalitarian solution ( $p = \infty$ ), which reduces the distance of the consensus to the worst-off member of the society.

In Section 4, we employ the general distance function in Eq. (6) to pose our problem of aggregating value systems as that of computing a consensus. By leveraging this general distance function, Section 6 analyses how the ethical principle determined by p (including the utilitarian and egalitarian principles) affects the consensus in particular case studies.

#### 3. Value systems: From theory to practice

Moral values are the principles deemed valuable by society [68] and involved in ethical choices [69]. Our preference over relevant, competing values guides our decision-making process [31]. To this extent, *value systems* are the structures employed to represent our moral values and associated preferences [29–31]. Rankings are typically used to describe value preferences because they are the less restrictive preference structure satisfying totality. However, recent works [8,38] contend that representing value systems solely as rankings is incomplete for concrete applications.

Computer scientists [8,34] and social scientists [32,33,35] argue that value systems are *contextual*. That is, the way in which we reason about and prioritise values is influenced by the context we are in. For instance, one may value freedom over safety but prioritise safety over freedom during a global pandemic [8]. Further, thinking about values is challenging for humans since it involves significant cognitive effort [70,71]. Thus, allowing humans to express their preferences over value-laden contextual alternatives (as opposed to competing values) is both easier and more insightful [72].

Along the lines of Gabriel [6], both Liscio et al. [8] and Lera-Leri et al. [38] consider value systems as *pluralistic*. As argued by Gabriel [6], humans hold various reasonable but contrasting beliefs about values. Therefore, we live in a pluralistic world where individuals ascribe to different value systems. Thus, individuals from different cultural backgrounds might judge the same action differently regarding the same moral value, which Lera-Leri et al. [38] describe as having different *value interpretations*. For instance, if we consider the moral value of *respect* in the context of a funeral, Western cultures consider wearing black as promoting the value (and failing to do it as demoting it), whereas Asian cultures favour a white dress code.

Considering the *contextuality* and *pluralism* of value systems, we identify four key elements that a value system must include:

- 1. a set of values relevant to the context under discussion;
- 2. a set of contextual **alternatives** (e.g., actions, policies) over which an individual ought to take value-laden choices;
- 3. a **relationship between alternatives and values** that captures value interpretation by specifying the degree to which an individual deems an alternative as *promoting* or *demoting* a value; and
- 4. a set of individual preferences over values.

On the one hand, the presence of alternatives and the relationship between alternatives and values delimit a context for situated value reasoning. On the other hand, the individual interpretation of the relationship between alternatives and values and consequent individual value preferences reflect the pluralism of values. To this extent, Chisholm [73] links these two aspects (i.e., alternatives or actions and values) by arguing that individuals may judge an action as either good or bad to perform (or not to perform) depending on the value under consideration.

Our goal is to aggregate value systems to obtain a consensus value system. To this end, we introduce two case studies aimed at estimating value systems (Sections 3.1 and 3.2). In each case study, we formally define the corresponding value system and show how individual value systems are obtained. Subsequently, in Section 6, we compute the consensus value system by aggregating both value interpretations and value preferences.

#### 3.1. Participatory value evaluation

Participatory Value Evaluation (PVE) [40] is a digital framework for eliciting citizens' preferences over governmental policy options. We use data from a PVE conducted in 2020 to gauge the opinion of the residents of a municipality in the Netherlands over energy policies [41].

The main question asked in this PVE was: *what do you find important for future decisions on energy policy*? As potential answers, six *policy options* were developed by policymakers in collaboration with a panel of 45 citizens. Each PVE participant was asked to distribute 100 points among the six options and then to motivate each option to which they had assigned points with a textual *motivation*. Table 1 shows the six

policy options and the mean points allocated to each option by the PVE participants.

The mean points allocated to each option in a PVE indicate *what* options the PVE participants prefer. However, these points do not indicate *why* the participants have that preference. To answer the why question, Siebert et al. [43] estimate the value system underlying each participant's preferences.

In Section 3.1.1, we describe how the previously introduced value system's four key components connect to this case study and provide a formal definition of a value system. In Section 3.1.2, we introduce the method that Siebert et al. [43] propose for estimating an individual's value system from their PVE data.

#### 3.1.1. Definition of value system

We adapt the definition of value system that Siebert et al. [43] propose to incorporate the four key components introduced earlier.

- 1. The value list V is the set of values relevant to the discussion.
- 2. The *alternatives* over which participants make value-laden choices are the policy options presented in the PVE (Table 1):  $O = \{o_1, \dots, o_6\}$ .
- 3. The *relationship between alternatives and values* captures value interpretation by means of a binary individual value-option matrix  $VO_i$  with |V| (number of values) rows and |O| (number of options) columns, where:

$$VO_i(v, o) = \begin{cases} 1, & \text{if value } v \text{ is relevant for an individual } i \text{ for option } o \\ 0, & \text{otherwise.} \end{cases}$$

In Section 3.1.2, we explain how an individual's  $VO_i$  is calculated based on their answers to the survey.

4. The *value preferences* are an individual's ranking  $R_i$  of V, which is a reflexive, transitive, and total binary relation, noted as  $v_a \geq v_b$ . Given  $v_a, v_b \in V$ , if  $v_a \geq v_b$ , we say  $v_a$  is more preferred than  $v_b$ . If  $v_a \geq v_b$  and  $v_b \geq v_a$ , then we note it as  $v_a \sim v_b$  and consider  $v_a$  and  $v_b$  indifferently preferred. However, if  $v_a \geq v_b$  but it is not true that  $v_b \geq v_a$  (i.e.,  $v_a \neq v_b$ ), then we note it as  $v_a > v_b$ .

Considering the four aspects, we define a value system in a PVE as follows.

**Definition 1.** A value system in a Participatory Value Evaluation is a tuple  $\mathcal{V}_i = \langle V, O, VO_i, R_i \rangle$ , where *V* is a non-empty set of values, *O* is a set of available policy options,  $VO_i$  is a matrix describing the relevance of a value for an individual for a given option, and  $R_i$  is the ranking of *V* which represents an individual's value preference.

#### 3.1.2. Value system estimation

The designers of the energy policy PVE identify the relevant values by analysing the participants' motivations for policy choices using a grounded theory approach. The five most commonly mentioned values they identified are: cost-effectiveness ( $v_1$ ), nature and landscape preservation ( $v_2$ ), leadership ( $v_3$ ), cooperation ( $v_4$ ), and self-determination ( $v_5$ ). However, these five values may not be relevant to each of the six policy options in Table 1.

Siebert et al. [43] propose computational methods for estimating a participant's value system based on the choices and motivations they provide in the PVE. They compute an initial *VO* matrix, shown in Table 2, as the first guess of value preferences based on the available choices in the PVE. It is intended to be the starting point for estimating the individual participants' value-option matrices (*VO<sub>i</sub>*) and value rankings ( $R_i$ ).

Siebert et al. [43] propose four methods for estimating participants' value systems. Their approach is based on the theory that "valuing is deliberatively consequential" [74]. That is, if a participant's choice is based on a deliberation of value preferences, the value preferences can be recognised in the motivation provided for the choice. The bestperforming approach is the sequential combination of three proposed methods (MO, MC, and TB):

Policy options in the	Policy options in the Súdwest-Fryslân PVE.						
Policy option	Description	Mean points					
<i>o</i> <sub>1</sub>	The municipality takes the lead and unburdens you	29.05					
<i>o</i> <sub>2</sub>	Inhabitants do it themselves	21.72					
0 <sub>3</sub>	The market determines what is coming	9.39					
$o_4$	Large-scale energy generation will occur in a small number of places	15.01					
05	Betting on storage (Súdwest-Fryslân becomes the battery of the Netherlands)	12.96					
<i>o</i> <sub>6</sub>	Become a major energy supplier in the Netherlands	4.71					

Table 1

VO matrices representing the relationship between alternatives and values.

(a)	(a) Initial VO for the energy transition PVE									
		Options								
	-	$o_1$	<i>o</i> <sub>2</sub>	03	$o_4$	$o_5$	06			
	$v_1$	1	1	1	1	1	1			
SS	$v_2$	1	1	0	1	1	1			
Values	$v_3$	1	1	1	0	0	0			
>	$v_4$	1	1	1	1	0	1			
	$v_5$	1	1	0	0	1	0			

- *MO* addresses inconsistencies between motivations provided for different choices. For example, consider that an individual selected options  $o_4$  and  $o_6$ , for which  $v_2$  and  $v_4$  are deemed relevant. Further, assume that they motivated  $o_4$  with value  $v_2$  and  $o_6$  with value  $v_4$ . Following the notion of valuing as deliberatively consequential, from the two motivations, one can both infer that  $v_2 > v_4$  and that  $v_4 > v_2$ . Thus, the method *MO* updates *VO<sub>i</sub>* by considering irrelevant the value that is part of the inconsistency but was not mentioned in the motivation (in practice, by setting the cells  $(v_4, o_4)$  and  $(v_2, o_6)$  to 0, as in Table 2).
- *MC* targets inconsistencies between choices and motivations. Assume that a participant allocates some points to option  $o_5$  where, according to *VO*,  $v_1$  is relevant, but  $v_4$  is not, but mentions  $v_4$  in the motivation. Then, *MC* adjusts *VO<sub>i</sub>* to prefer  $v_4$  over  $v_1$  for  $o_5$  (in practice, by setting the cell ( $v_1, o_5$ ) to 0 and the cell ( $v_4, o_5$ ) to 1, as in Table 2).
- *TB* reduces the number of indifferent preferences in an individual's value ranking. First, it computes the importance of values for an individual by weighing the values supported in  $VO_i$  with the points that the participant assigned to the options. For instance, consider that individual *i* distributes their points to the six policy options as: {30, 40, 10, 20, 0, 0}. The multiplication of  $VO_i$  by the vector of this policy scores results in a vector of importance scores for values in V: {100, 90, 80, 80, 70}. Then, the individual's value ranking  $R_i$  is inferred by ordering the values in V according to their importance score:  $v_1 > v_2 > v_3 \sim v_4 > v_5$ , where  $v_a \sim v_b$  indicates that there is a tie, i.e., the participant has no preference between  $v_a$  and  $v_b$ . However, if one of the motivations mention  $v_3$ , then the *TB* method breaks the tie by setting  $v_4 > v_3$ , thus resulting in  $R_i : v_1 > v_2 > v_3 > v_5$ .

#### 3.2. European value study

The European Values Study (EVS) [42] is a large-scale survey research programme on European values. It collaborates with the World Values Survey [75]. The programme provides data about the variety of positions that citizens from different European countries have on basic values such as well-being, solidarity, and democracy. Although the EVS survey covers a wide range of questions and values, here we focus on two values and three questions for 34 European countries. Our goal is not to comprehensively analyse European values but to illustrate our aggregation approach with a simplified example.

(h)	Evampla	of	actimated	individual	VO

		Options							
		$o_1$	<i>o</i> <sub>2</sub>	03	$o_4$	$o_5$	06		
	$v_1$	1	1	1	1	0	1		
SS	$v_2$	1	1	0	1	1	0		
Values	$v_3$	1	1	1	0	0	0		
>	$v_4$	1	1	1	0	1	1		
	$v_5$	1	1	0	0	1	0		

3.2.1. Definition of value systems

We adopt the definition of Value System  $\mathcal{V}$  for the EVS from Lera-Leri et al. [38] and identify the four key elements of this value system.

- 1.  $V = \{v_1, \dots, v_n\}$  is the set of values relevant to European citizens.
- 2. The alternatives are a set of actions,  $A = \{a, ..., a_m\}$ , which give information about the value interpretation of citizens.
- 3. We relate values with actions to interpret each value  $v \in V$  for every country *i*. To do so, for each value  $v \in V$  and the actions in *A*, we define the action judgement function  $a_v^i : A \rightarrow [-1, 1]$  for country *i* as the function that evaluates the promotion or demotion of value v when performing action  $a \in A$ . These evaluations are real numbers in the interval [-1, 1]: a positive number indicates the degree to which a value is being promoted, whereas a negative one indicates demotion. For instance, in the "funeral dress code" example from Section 3, a western-raised individual would consider wearing black clothes (wbc) as an action that promotes the value respect ( $a_{respect}^i(wbc) > 0$ ), and wearing colourful clothes (wcc) is an action that demotes the value respect ( $a_{respect}^i(wbc) < 0$ ). We represent such evaluations in a value-action matrix such that

$$VA_{i} = \begin{bmatrix} \alpha_{v_{1}}^{i}(a_{1}) & \cdots & \alpha_{v_{1}}^{i}(a_{m}) \\ \vdots & \ddots & \vdots \\ \alpha_{v_{n}}^{i}(a_{1}) & \cdots & \alpha_{v_{n}}^{i}(a_{m}) \end{bmatrix},$$
(5)

where each row corresponds to the action judgement functions of a value.

4. We define a country *i*'s value preferences via a preference matrix  $P_i \in [0,1]^{n \times n}$ , where  $P_i[v_j, v_k] \in [0,1]$  represents *i*'s graded preference when comparing  $v_j$  and  $v_k$ . The value preferences in  $P_i$  are *pairwise comparisons*, where 0.5 stands for indifference. For instance, individuals from a country may prefer environmental protection over economic development with a grade of 0.75.

Given these elements, we formally define the value system as follows.

**Definition 2.** Given a set of values *V* and a set of actions *A*, a value system for the European Values Study is a tuple  $\mathcal{V}_i = \langle V, A, VA_i, P_i \rangle$  for individual *i*, where  $VA_i$  is the value-action matrix containing the evaluation of values with relation to actions, and  $P_i$  is the preference matrix containing the preference pairwise comparisons between values.

Value preferences (columns 2 and 3) and value judgement functions (columns 4-7) for a subset of countries in the EV	VS.
---	-----

Country	$P_i[rl, pr]$	$P_i[pr, rl]$	$\alpha^i_{rl}(ho)$	$\alpha^i_{rl}(dv)$	$\alpha^i_{pr}(ho)$	$\alpha^i_{pr}(dv)$
🔁 сн	0.32	0.68	0.01	0.20	0.30	0.56
≽ cz	0.22	0.78	-0.09	0.01	0.12	0.32
📒 DE	0.36	0.64	0.20	0.25	0.42	0.59
DK DK	0.24	0.76	0.25	0.53	0.46	0.75
EE	0.26	0.74	-0.52	-0.07	-0.23	0.24
ES ES	0.40	0.60	0.15	0.20	0.44	0.50
🛨 FI	0.35	0.65	0.02	0.30	0.32	0.62
FR FR	0.36	0.64	0.29	0.26	0.51	0.54
GB	0.38	0.62	0.20	0.20	0.39	0.50
🕂 GE	0.94	0.06	-0.71	-0.50	-0.60	-0.32
🚬 HR	0.61	0.39	-0.41	-0.17	-0.02	0.28
NL NL	0.32	0.68	0.26	0.19	0.52	0.63

#### 3.2.2. Value system estimation

We resort to the EVS data [76] to create the value system of each country. We consider two values: religiosity (rl) and permissiveness (pr).<sup>3</sup> We characterise these two values in terms of their action judgement functions. For simplicity, we consider the judgement of two actions: homosexual couples' parenthood ( $h_0$ ) and divorcing (dv). To characterise Europeans' position on religiosity, we consider the EVS question "Q1F: How important is religion in your life?" and partition possible answers so that we can discern the percentage of citizens who consider religion important from the ones who do not. Columns 2 and 3 of Table 3 show the respective percentages per country, which we also interpret as the degree of preference of each value. For conciseness, Table 3 lists 12 out of the 34 countries considered in our computation. Formally, we denote the preference degree of value rl over pr in country i as  $P_i[rl, pr]$ . Conversely, we denote as  $P_i[pr, rl]$  the preference degree of pr over rl. As a consequence, we assume that those countries in which religion is important for the majority of the population (i.e.,  $P_i[rl, pr] > P_i[pr, rl]$ ) will prefer religiosity over permissiveness, whereas we consider that permissiveness is preferred over religiosity if  $P_i[rl, pr] < P_i[pr, rl]$ .

Next, we employ two additional EVS questions to characterise the value judgement functions of the values under consideration: "Q27A: How much do you agree or disagree with the statement: Homosexual couples are as good parents as other couples?" and "Q44G: Can divorce be always justified, never justified, or something in between?". By correlating these answers with those about religion, we obtain the judgements of religious citizens of each country on homosexual parenthood and divorce (columns 4–5 of Table 3). Similarly, we obtain the judgements of non-religious people (columns 6–7 of Table 3).

## 4. Formalising the aggregation of value systems

After formally describing a value system  $\mathcal{V}$  and two real-world examples, we proceed to the problem of aggregating value systems,  $\mathcal{V}_1, \ldots, \mathcal{V}_N$ , of individuals  $i = 1, \ldots, N$ . Specifically, we compute a value system  $\mathcal{V}_S$  that *best* represents the aggregation of  $\mathcal{V}_1, \ldots, \mathcal{V}_N$  according to an *ethical principle* p.<sup>4</sup>

Recall that a value system has four key components. We assume that the first two components, the set of values and the set of alternatives, are the same across all individuals. So it is not necessary to aggregate them. Then, the problem of aggregating multiple value systems boils down to aggregating the last two components, the relationship between values and alternatives and the value preferences, which are specific to the individuals.

We pose the overall aggregation problem as a two-step procedure to compute: (1) a *consensus* values-alternatives relation, and (2) a *consensus* of preferences over values. We represent the objects for aggregation (i.e., the individual values-alternatives relations and the individual preferences over values) as *q*-dimensional vectors. This representation provides sufficient expressiveness since it generalises 1-dimensional vectors and matrices, which are commonly used in the literature [44, 55–57] and in the test cases described in Sections 3.1 and 3.2 for these purposes.

Considering a unique general representation for individual objects allows us to pose the aggregation problem in a unique general way. Following the social choice literature (Section 2), we cast this problem as the minimisation of a distance measure defined along the lines of Eqs. (1) and (2) (for 1 and 2-dimensional cases, respectively). To accommodate a *q*-dimensional representation, we generalise these distance functions as:

$$U_p = \left[\sum_{i=1}^n \sum_{j_1=1}^{J_1} \cdots \sum_{j_q=1}^{J_q} w_i |T_i[j_1, \dots, j_q] - T_S[j_1, \dots, j_q]|^p\right]^{1/p},$$
(6)

where  $T_i[j_1, \ldots, j_q]$  is the judgement or preference value provided by the *i*th member of the society to the particular combination over qfeatures.<sup>5</sup> Notice that the generalisation that we propose in Eq. (6) does not assume any underlying vectorial structure. We propose such generalisation to aggregate vectors, matrices, q-dimensional vectors, and even scalars when considered as one-component vectors.

Following Definition 1, Eq. (6) can be readily particularised for the PVE case study to define the distance between the individual valueoption matrices  $VO_i$  and the aggregated value-option matrix  $VO_S$  as

$$U_{p}^{(VO)} = \left[\sum_{i=1}^{N} w_{i} \sum_{j=1}^{|V|} \sum_{k=1}^{|O|} \left| VO_{i}[v, o] - VO_{S}[v, o] \right|^{p} \right]^{1/p}.$$
(7)

<sup>&</sup>lt;sup>3</sup> Although the values of *religiosity* [77] and *permissiveness* [78] can be related to the values of *tradition* and *tolerance* from the Schwartz's revised model of values [79], we choose them to fit EVS's data better. In fact, one may even think that secularism seems a better alternative to permissiveness when comparing it to religiosity. However, we argue that permissiveness [78] is better suited, as it is specifically related to sexual freedom [80], and the data from EVS we use relates to homosexual couples and divorce.

<sup>&</sup>lt;sup>4</sup> We refer to p as the ethical principle used to compute the aggregation, in accordance with the social choice literature (Section 2). This should not be confused with the objects of our aggregation, i.e., the value systems.

<sup>&</sup>lt;sup>5</sup> The judgements or preferences of the individuals  $T_i[j_1, ..., j_q]$  can be represented with binary, integer or real numbers, depending on the case study domain.

From Eq. (6), we can also derive a definition for the distance between the individual rankings  $R_i$  and the aggregated ranking  $R_S$  as

$$U_{p}^{(R)} = \left[\sum_{i=1}^{N} w_{i} \sum_{j=1}^{|V|} \left| R_{i}[j] - R_{S}[j] \right|^{p} \right]^{1/p}.$$
(8)

Definitions for the EVS case can be derived similarly. We do not report these definitions for the sake of conciseness.

For a general value system defined in Section 3, we denote the distance function referring to the relationships between values and alternatives, and the value preferences as  $U_p^{(3)}$  and  $U_p^{(4)}$ , respectively. Then, we can pose *value system aggregation* as a two-step problem aiming to compute

$$T_{S}^{(3)} = \arg\min U_{p}^{(3)},$$
 (9)

$$T_S^{(4)} = \arg\min U_p^{(4)},$$
 (10)

where  $T_S^{(3)}$  and  $T_S^{(4)}$  denote the consensus among values-alternatives relationships and value preferences, respectively.

## 5. An $\ell_p$ -regression approach to aggregate value systems

We show how Eqs. (9) and (10) can be cast as  $\ell_p$ -regression (also known as *norm approximation* [46]) problems. Such a transformation yields obvious computational benefits as it allows us to efficiently solve the above-mentioned optimisation problems for any *p*, as explained in Section 5.1.

Since solving Eqs. (9) and (10) can be seen as the minimisation of the same general q-dimensional distance function (i.e., Eq. (6)), in Theorem 5.1 we directly consider this problem.

**Theorem 5.1.** Computing the solution  $T_S = \arg \min U_p^{(T)}$  is equivalent to computing the solution x of the  $\ell_p$ -regression problem

minimise 
$$||Ax - b||_p$$
, (11)  
where  $A \in \mathbb{R}^{N \cdot J_1 \cdots J_q \times J_1 \cdots J_q}$  and  $b \in \mathbb{R}^{N \cdot J_1 \cdots J_q}$  are

 $A = \begin{bmatrix} w_1^{1/p} \cdot I \\ \vdots \\ w_N^{1/p} \cdot I \end{bmatrix}, \quad b = \begin{bmatrix} w_1^{1/p} \cdot \overrightarrow{T_1} \\ \vdots \\ w_N^{1/p} \cdot \overrightarrow{T_N} \end{bmatrix},$ 

 $I \in \mathbb{R}^{J_1 \cdot J_2 \cdots J_q \times J_1 \cdot J_2 \cdots J_q}$  is the identity matrix of size  $J_1 \cdot J_2 \cdots J_q$ ,  $\overline{(\cdot)}$  is the vectorisation operation that turns a *q*-dimensional vector into a 1-dimensional vector, and the *p*-norm  $||x||_p$  of a vector *x* is defined as  $||x||_p = (\sum_i |x[i]|^p)^{1/p}$ .

**Proof.** As a first step, we rewrite Eq. (6) as

$$\left[\sum_{i=1}^{N} w_{i} \sum_{h=1}^{J_{1} \cdot J_{2} \cdots J_{q}} \left| T_{i}[h] - T_{S}[h] \right|^{p} \right]^{1/p}$$
(12)

and, subsequently, as

$$\left[\sum_{i=1}^{N} \left\| w_{i}^{1/p} \cdot \overrightarrow{T}_{i} - w_{i}^{1/p} \cdot \overrightarrow{T_{S}} \right\|_{p}^{p} \right]^{1/p}.$$
(13)

To express Eq. (13) as an  $\ell_p$ -regression problem, we define  $A \in \mathbb{R}^{N \cdot J_1 \cdot J_2 \cdots J_q \times J_1 \cdot J_2 \cdots J_q}$  and  $b \in \mathbb{R}^{N \cdot J_1 \cdot J_2 \cdots J_q}$  as

$$A = \begin{bmatrix} w_1^{1/p} \cdot I \\ \vdots \\ w_N^{1/p} \cdot I \end{bmatrix}, \quad b = \begin{bmatrix} w_1^{1/p} \cdot \overrightarrow{T_1} \\ \vdots \\ w_N^{1/p} \cdot \overrightarrow{T_N} \end{bmatrix},$$

We can finally formulate the problem of minimising Eq. (6) as

minimise  $||Ax - b||_p$ .

The solution of the above-defined problem (i.e., the vector *x*) is  $T_S$ .

#### 5.1. Solving the $\ell_p$ -regression problem

We now discuss a computational solution to Eq. (11). This solution applies to aggregating both case studies' value-alternative relations and value preferences, as particular cases of Eq. (11).

For p = 1, Eq. (11) represents an absolute residuals approximation problem. For  $p = \infty$ , we are dealing with a *Chebyshev approximation* (or *Min-Max approximation*) problem. In both cases, Eq. (11) can be solved via *Linear Programming* [46]. For p = 2, Eq. (11) can be solved analytically by treating it as *Least Squares* problem,<sup>6</sup> whose optimal solution is

$$x = (A^T A)^{-1} A^T b. (14)$$

We employ this analytical solution in Theorem 5.2, where we show that, for p = 2, the aggregation of a general *q*-dimensional vector can be obtained as the *weighted arithmetic mean* of the individual *q*-dimensional vectors  $(T_1, ..., T_N)$ .

**Theorem 5.2.** For p = 2,  $T_S$  can be analytically computed as the weighted arithmetic mean of the individual T *q*-dimensional vectors  $(T_1, \ldots, T_N)$ , where the weights are  $w_1, \ldots, w_N$ .

**Proof.** As a first step, we explicitly compute  $(A^T A)^{-1}$  as

$$(A^{T}A)^{-1} = \left( \begin{bmatrix} w_{1}^{1/2} \cdot I & \cdots & w_{N}^{1/2} \cdot I \end{bmatrix} \begin{bmatrix} w_{1}^{1/2} \cdot I \\ \vdots \\ w_{N}^{1/2} \cdot I \end{bmatrix} \right)^{-1}$$
  
$$= \left( \sum_{i=1}^{N} w_{i} \cdot I \right)^{-1} = \left( \sum_{i=1}^{N} w_{i} \right)^{-1} I.$$
 (15)

Notice that Eq. (15) is a diagonal matrix whose elements in the diagonal are all equal to the inverse of the sum of the weights. By making use of the above result, we explicitly compute *x* as

$$x = \left(\sum_{i=1}^{N} w_i\right)^{-1} \underbrace{\left[w_1^{1/2} \cdot I \cdots w_N^{1/2} \cdot I\right]}_{\sum_{i=1}^{N} w_i} \begin{bmatrix}w_1^{1/2} \cdot \overrightarrow{T_1} \\ \vdots \\ w_N^{1/2} \cdot \overrightarrow{T_N} \end{bmatrix}$$

$$= \frac{\sum_{i=1}^{N} w_i \cdot \left[\overrightarrow{T_i}\right]}{\sum_{i=1}^{N} w_i} = \frac{\sum_{i=1}^{N} w_i \cdot \overrightarrow{T_i}}{\sum_{i=1}^{N} w_i}.$$
(16)

Thus, each element of x (i.e., of  $T_S$ ) is the weighted mean of the corresponding elements of  $T_i$ , according to the weights  $w_1, \ldots, w_N$ .

For any  $p \notin \{1, 2, \infty\}$ , Eq. (6) represents a non-linear problem. Nonetheless, by exploiting the structure of Eq. (11) as an  $\ell_p$ -regression problem, we can solve it for any *p*. To do so, we choose the state-of-theart *Iteratively Reweighted Least Squares* (IRLS) algorithm [45], the only approach for  $\ell_p$ -regression that is guaranteed to converge for any value of *p*.<sup>7</sup>

### 6. Experimental results

We empirically investigate our method for computing the consensus value systems for the case studies in Sections 3.1 and 3.2. Our analysis shows that our approach is flexible enough to aggregate value preferences encoded differently (i.e., as value rankings in the PVE and pairwise comparisons in the EVS case study). In particular, we aim to:

<sup>&</sup>lt;sup>6</sup> The Least Squares problem is obtained by squaring the objective of the original  $\ell_2$ -regression problem. The obtained problem is equivalent to the original one (i.e., it has the same optimal solution), but it has the advantage that it can be solved analytically by expressing the objective as a convex quadratic function [46].

<sup>&</sup>lt;sup>7</sup> Our source code: https://github.com/RogerXLera/ValueSystemsAggregat ion. We use the publicly-available IRLS code [45]: https://github.com/fastalgos/pIRLS.

- 1. Illustrate how the choice of a given ethical principle (from 1 to  $\infty$ ) affects the resulting consensus value system;
- Understand the impact of employing different social weights for the individual value systems on the resulting consensus value system;
- 3. Analyse the classification of the available ethical principles based on the *proximity* of the consensus they produce with respect to the utilitarian and egalitarian consensuses; and
- 4. Study at a fine-grained level how the relationship between the distribution of individual value systems and the resulting consensus varies (with respect to the majority and the minority) as the value of the ethical principle increases.

Finally, we distill our empirical analysis to delineate the guidelines a policymaker should follow in choosing an ethical principle when performing the aggregation of ethical principles.

In Sections 6.1 and 6.2, we analyse the results for the two case studies, respectively, to address the first two goals. Then, Section 6.3 tackles the characterisation of the space of ethical principles as pursued by the third goal. Finally, Section 6.4 investigates the relationship between consensus and individuals as the ethical principle changes (i.e., 4th goal).

#### 6.1. Case study: Participatory value evaluation

The PVE case study comprises five values, six options, and 795 individual value systems estimated via the method in Section 3.1.2. In aggregating these value systems, we treat all individuals as equal within society. Thus, all individuals have the same weight in the distance functions employed to compute the consensus among values-alternatives relationships and value preferences in Eqs. (9) and (10), i.e.,  $\forall i \in \{1, 2, ..., 795\}, w_i = 1$ .

## 6.1.1. Analysing the consensus on value preferences

We show the results of aggregating the rankings over values corresponding to the 795 individual value systems according to different ethical principles.

**Encoding individual value preferences.** First, we build the ranking of values for each individual. For each individual *i*, we set  $R_i[v_j]$  to the position of value  $v_j$  in *i*'s ranking. For two values,  $v_j$  and  $v_k$ , that are equally preferred, we assign the same position within the ranking, i.e.,  $R_i[v_j] = R_i[v_k]$ .

**Aggregating individual value preferences.** Next, we compute the consensus ranking  $R_S$  by solving Eq. (10) for distance function in Eq. (8), following the method in Section 5.1. When computing the consensus, we do not enforce the position of a value j to be an integer. Thus, for instance, a consensus of  $R_S[v_j] = 2.5$  indicates that the society considers that value  $v_j$  has a position between the second and third position in the consensus ranking. We consider that value  $v_j$  is preferred over value  $v_k$  ( $v_j > v_k$ ) when their positions in the consensus ranking differ such that  $R_S[v_k] - R_S[v_j] > \epsilon$ , where  $\epsilon$  is a small positive number ( $\epsilon = 0.05$  in our experiments). Otherwise, we say the two values are equally preferred or indifferent ( $v_j \sim v_k$ ).

Table 4 shows the consensus rankings resulting from the aggregation of individual rankings for different ethical principles (*p*): from 1 (utilitarian) to 10, and  $\infty$  (egalitarian). Each column  $R_S[v_i]$  indicates the position of value  $v_i$  in the ranking computed by our aggregation. Note that we obtained a partial ranking as a consensus ranking for each ethical principle. That is, the order (preferences) between values in each consensus ranking is not strict since it contains ties between values. For instance, in the first row, value  $v_1$  is equally preferred to value  $v_2$  (because  $R_S[v_1] = R_S[v_2] = 2$ ).

From Table 4, we distinguish three types of consensus rankings.

• p = 1 (utilitarian):  $v_1$  and  $v_2$  are equally preferred. They are both preferred over the others ( $v_3, v_4, v_5$ ), which are equally preferred.

- $p \in [2..10]$  (intermediate):  $v_1$  becomes more preferred than  $v_2$ , while both are still more preferred than the rest of values  $(v_3, v_4, v_5)$ . The indifference between  $v_3, v_4$  and  $v_5$  holds.
- $p = \infty$  (egalitarian): all values are equally preferred.

We make two interesting observations from Table 4. First, recall (Section 5.1) that for p = 2, the consensus ranking results from computing the mean of the individual rankings to aggregate. Thus, our consensus ranking for p = 2 is the same as obtained by Siebert et al. [43], which solely employs the mean of individual rankings to compute a consensus ranking. Second, the consensus position  $R_S$  for all moral values converges to 3 (central position in the ranking) as the value of parameter p increases.

#### 6.1.2. Analysing the consensus on values-alternatives relationships

After analysing the impact of choosing different ethical principles on the consensus value preferences, we now discuss the results of the consensus value-option matrices. Recall from Section 3.1.2 that each individual holds a different view of the relationship between values and options. Computing the consensus on the value-option matrices unveils the most representative value-option matrix (i.e., the most representative interpretation of values) on which the consensus value preferences apply. Recall (Section 3.1.1) that the binary value-option matrix  $VO_i$  indicates whether a value v is promoted by option o or not according to individual i. We remark that considering binary matrices for expressing the relationship between values and alternatives is the result of applying the methodology proposed by Siebert et al. [43]. However, in the EVS case study presented in the following section, we will discuss a different instance of the relationship between alternatives and values that contain more gradual evaluations [-1,1], representing the degree of promotion or demotion of a given value when performing a specific action.

For brevity, we only analyse the consensus in three cases of interest: the utilitarian (p = 1), the *mean principle* (p = 2), and the egalitarian ( $p = \infty$ ) cases. For ease of understanding, we first discuss the mean principle case.

**Mean principle** (p = 2). Eq. (17) shows the resulting consensus valueoption matrix. From Theorem 5.2, we know that aggregating individual value-option matrices results in a value-option matrix containing the mean values of the individual matrices. By multiplying the consensus value-option matrix by 100, we obtain the percentage of individuals considering value v relevant for option o. For example,  $v_3$  is deemed relevant to 45.2% of the participants to justify option  $o_1$ ; similarly,  $v_5$ and  $v_2$  are related to options  $o_2$  and  $o_4$ , respectively, for more than 30% of the participants.

**Utilitarian principle** (p = 1). The consensus value-option matrix  $VO_S$  is a zero matrix, i.e.,  $VO_S[v, o] = 0$  for every value  $v \in V$  and option  $o \in O$ . This indicates that no value  $v \in V$  is promoted in any option  $o \in O$ . Despite Table 2 showing that there are values that are frequently annotated for some options, most individual value-option matrices are sparse (have many zeros). This is reflected in Eq. (17), where there are no options in which a majority of individuals indicated a specific value to be relevant (i.e., no entry of Eq. (17) is larger than 0.5). This leads the method to compute a consensus of zeros because  $\ell_1$ -regression tends to have residuals  $(VO_i[v, o] - VO_S[v, o])$  equal to 0. This is well-known in the optimisation literature [46].

Tuble 1							
Computed	consensus	ranking	for	different	ethical	principles	n

r										
р	$R_S[v_1]$	$R_{s}[v_{2}]$	$R_{S}[v_{3}]$	$R_S[v_4]$	$R_{S}[v_{5}]$	Consensus ranking				
1	2.00	2.00	3.00	3.00	3.00	$v_1 \sim v_2 \succ v_3 \sim v_4 \sim v_5$				
2	2.14	2.53	2.90	2.90	2.91	$v_1 \succ v_2 \succ v_3 \sim v_4 \sim v_5$				
3	2.31	2.65	2.95	2.96	2.94	$v_1 \succ v_2 \succ v_3 \sim v_4 \sim v_5$				
4	2.42	2.73	2.97	2.98	2.96	$v_1 \succ v_2 \succ v_3 \sim v_4 \sim v_5$				
5	2.51	2.78	2.98	2.99	2.97	$v_1 > v_2 > v_3 \sim v_4 \sim v_5$				
6	2.58	2.81	2.99	3.00	2.98	$v_1 \succ v_2 \succ v_3 \sim v_4 \sim v_5$				
7	2.63	2.84	2.99	3.00	2.98	$v_1 \succ v_2 \succ v_3 \sim v_4 \sim v_5$				
10	2.74	2.89	2.99	3.00	2.99	$v_1 \succ v_2 \succ v_3 \sim v_4 \sim v_5$				
$\infty$	3.00	3.00	3.00	3.00	3.00	$v_1 \sim v_2 \sim v_3 \sim v_4 \sim v_5$				

Table 4

Value preferences (columns 2, 3, and 8) and value judgement functions (columns 4–7) of the consensus European value system when considering equal social influence.

р	$P_S[rl, pr]$	$P_S[pr, rl]$	$\alpha_{rl}^S(ho)$	$\alpha_{rl}^S(dv)$	$\alpha_{pr}^{S}(ho)$	$\alpha_{pr}^{S}(dv)$	Value pref.
1	0.504	0.496	-0.288	0.013	-0.054	0.318	rl > pr
2	0.535	0.465	-0.224	0.031	-0.032	0.315	rl > pr
3	0.548	0.452	-0.200	0.029	-0.029	0.280	rl > pr
$\infty$	0.580	0.420	-0.148	0.027	-0.077	0.159	rl > pr

**Egalitarian principle**  $(p = \infty)$ . The consensus value-option matrix has  $VO_S[v, o] = 0.5$  for every value  $v \in V$  and option  $o \in O$ . This is because the egalitarian principle minimises the disagreement with the most displaced elements of the society, i.e., the distance between the consensus for each value-option pair and the individuals assigning the largest and lowest judgement to the value-option pair. Recall from Table 2 that our value-option matrices are binary. By peeking into the individual option matrices, we observe that for every value-option pair (v, o), the maximum  $VO_i[v, o]$  is 1 (at least one individual mentions value v to justify option o). The minimum  $VO_i[v, o]$  is 0. Hence,  $VO_S[v, o] = 0.5$  for every moral value  $v \in V$ , and option  $o \in O$  because 0.5 is the consensus value that minimises the distance to the most displaced individual.

#### 6.2. European value study

We now study the aggregation of value systems for the European Values Study case. Similar to the PVE case, we explore how the resulting value system is affected by the parameters of our aggregation approach. However, unlike the PVE case, in the EVS case, we consider two cases for social influence: (1) where all countries have the same influence ( $w_i = 1$ ), and (2) where social influence  $w_i$  of a country *i* is proportional to the population of that country (i.e.,  $w_i = population_i/\Sigma_i population_i$ ).<sup>8</sup>

Recall from Section 3.2 that this case considers 34 European countries, two values (religiosity (rl) and permissiveness (pr)), and two actions (divorce (dv) and parenthood by homosexual couples (ho)). Tables 5 and 6 show the consensus value systems for different ethical principles, considering equal and population-based social influence, respectively. We report results for the utilitarian (p = 1) and egalitarian cases  $(p = \infty)$  and p = 2 and p = 3. We choose to show these values of parameter p as a change of value preferences can be observed in the consensus computed with p = 2 and p = 3 in the population-based social influence scenario (Table 6). In both tables,  $P_S$  stands for the value of the consensus on moral value preferences, whereas the  $\alpha$  values contain the consensus values on moral value-action relationships. For instance,  $P_{S}[rl, pr]$  indicates the consensus grade of preference of the religiosity moral value over the permissiveness moral value. Further,  $\alpha_{rl}^{S}(dv)$  denotes the consensus grade of promotion of the religiosity value when performing action divorce.

**Equal social influence.** In Table 5, all countries have the same social influence. We observe that all the *consensus European value systems* prefer religiosity over permissiveness. This is because the computed preference of religiosity over permissiveness is larger than 0.5 ( $P_S[rl, pr] > 0.5$ ) for all ethical principles (p) considered. However, for the utilitarian case (p = 1), this preference is barely noticeable (i.e., both  $P_S[rl, pr]$  and  $P_S[pr, rl]$  are close to 0.5), whereas the difference between  $P_S[rl, pr]$  and  $P_S[pr, rl]$  increases as we increase the value of parameter p. This transition happens because, for greater values of p, the consensus tends to reduce the maximum disagreement with the most "extreme" preferences, which in our case is by Georgia ( $P_i[rl, pr] = 0.94$ ). In addition, for all p's the parenthood by homosexual couples is valued negatively (see the values of  $\alpha_{rl}^S(ho)$  and  $\alpha_{pr}^S(ho)$ ), whereas divorce is slightly accepted (see the values of  $\alpha_{rl}^S(dv)$  and  $\alpha_{pr}^S(dv)$ ).

**Population-based social influence.** When considering social influence based on population size (Table 6), we observe significant changes compared to the previous case. Specifically, for the utilitarian principle (p = 1), permissiveness is preferred over religiosity (since  $P_S[pr,rl]$  is larger than  $P_S[rl, pr]$ ) and both adoptions by homosexual couples and divorce promote both values. This consensus shift is due to the social influence that highly populated European countries, such as Germany, France, and Great Britain, wield, which prefer permissiveness over religiosity. Nonetheless, as we increase p, we obtain the same transition towards religiosity as observed in Table 5. Indeed, for values of parameter p equal or larger than 3 we obtain the same trend on all consensus values (for  $P_S$  and  $\alpha$ ) for both the population-based (weighted) and the equal social influence (unweighted) cases. This confirms that the impact of weights ( $w_i$ ) vanishes when considering high values of parameter p in accordance with Eq. (4).

Overall, choosing the aggregation parameters (p and  $w_i$ ) determines between swaying towards prevailing (majority) value systems or value systems that lay closer to divergent opinions. In the EVS case, we even obtain a swap for the preferences of *religiosity* and *permissiveness*.

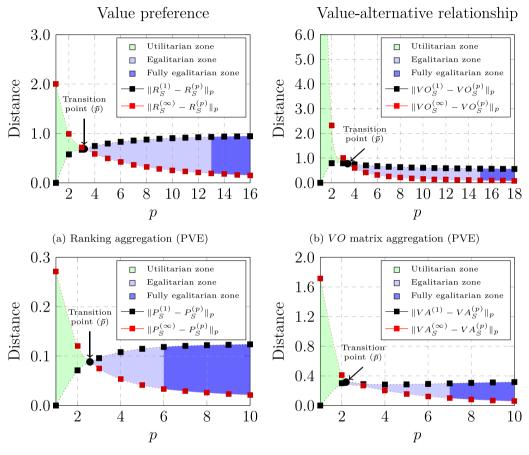
#### 6.3. Characterising the space of ethical principles

We characterise the *whole* space of ethical principles (from utilitarian to egalitarian) available to a decision-maker when computing a consensus value system. We do so to determine whether an ethical principle *p* produces a consensus leaning towards utilitarian (*p* = 1) or egalitarian (*p* =  $\infty$ ). To achieve our objective in the PVE case, we compute the consensus ranking *R*<sub>S</sub> considering a given *p* (denoted as *R*<sup>(*p*)</sup><sub>S</sub>). We measure the distance between *R*<sup>(*p*)</sup><sub>S</sub> and the one corresponding to *p* = 1 and *p* =  $\infty$ , denoted as *R*<sup>(1)</sup><sub>S</sub> and *R*<sup>(∞)</sup><sub>S</sub> respectively. Formally,

<sup>&</sup>lt;sup>8</sup> The population data is accessed from *Worldometers* (https://www. worldometers.info/world-population/population-by-country) in Sept. 2021.

Value preferences (columns 2, 3, and 8) and value judgement functions (columns 4–7) of the consensus European value system when social influence considers population.

р	$P_S[rl, pr]$	$P_S[pr, rl]$	$\alpha_{rl}^S(ho)$	$\alpha_{rl}^S(dv)$	$\alpha_{pr}^{S}(ho)$	$\alpha_{pr}^{S}(dv)$	Value pref.
1	0.444	0.556	0.007	0.123	0.187	0.503	pr > rl
2	0.495	0.505	-0.128	0.111	0.059	0.400	pr > rl
3	0.521	0.479	-0.154	0.080	0.015	0.364	$rl \succ pr$
8	0.580	0.420	-0.148	0.027	-0.077	0.159	$rl \succ pr$



(c) Value preference matrix aggregation (EVS)

(d) VA matrix aggregation (EVS)

**Fig. 2.** Distance between the consensus computed according to ethical principle p and the consensuses computed according to p = 1 (fully utilitarian, black line) and  $p = \infty$  (fully egalitarian, red line). The transition point  $\bar{p}$  is the ethical principle producing a consensus equidistant from the fully utilitarian and fully egalitarian ones. Thus,  $\bar{p}$  divides the space of ethical principles into an *utilitarian zone* (more similar to the fully utilitarian consensus, green) and an *egalitarian zone* (more similar to the fully egalitarian consensus, light blue). The *fully egalitarian* (dark blue) zone marks the ethical principles that produce a consensus approximately equal (to a small  $\epsilon$ ) to the fully egalitarian one. PVE case study on top, and EVS case study for the population-based influence case at the bottom.

we denote these two distances as  $\|R_S^{(1)} - R_S^{(p)}\|_p$  and  $\|R_S^{(p)} - R_S^{(\infty)}\|_p$ . Analogously, we define  $\|VO_S^{(1)} - VO_S^{(p)}\|_p$  and  $\|VO_S^{(p)} - VO_S^{(\infty)}\|_p$  for value-option matrices. In the same vein, for the EVS case, we denote the distances between value preferences as  $\|P_S^{(1)} - P_S^{(m)}\|_p$  and  $\|P_S^{(p)} - P_S^{(m)}\|_p$ , and denote the distances between value-action matrices as  $\|VA_S^{(p)} - VA_S^{(p)}\|_p$  and  $\|VA_S^{(p)} - VA_S^{(m)}\|_p$ . By making use of the above-defined distances, we can determine a

By making use of the above-defined distances, we can determine a *transition point* (denoted as  $\bar{p}$ ) that is the equidistant ethical principle whose computed consensus is between the fully utilitarian and the fully egalitarian consensuses. In addition, we define the *limit point*,  $\hat{p}$ , as the ethical principle such that all  $p > \hat{p}$  produce a consensus that is approximately equal (to a small  $\epsilon$ ) to the fully egalitarian one ( $p = \infty$ ). We compute  $\hat{p}$  that satisfies:

$$\frac{U_{p-1}^{(R)} - U_p^{(R)}}{U_p^{(R)}} < \epsilon,$$

where  $U_p^{(R)}$  is the value of the distance function defined by Eq. (8).

Because of the transition and limit points, we can characterise different zones within the space of ethical principles as Fig. 2 illustrates.

- The *utilitarian zone* is composed of all ethical principles leaning towards the fully utilitarian case (*p* < *p*).
- The *egalitarian zone* is composed of all ethical principles leaning towards the fully egalitarian case but before surpassing the *limit point* (*p̂*), i.e., *p* ∈ [*p̄*.*p̂*].
- The *fully egalitarian zone* is composed of the set of all ethical principles greater than the limit point, i.e.,  $p > \hat{p}$ .

Fig. 2(a) plots the distances between the consensus ranking  $(R_S^{(p)})$  with respect to the fully utilitarian  $(R_S^{(1)})$  and fully egalitarian consensus rankings  $(R_S^{(\infty)})$  as the value of the ethical principle *p* increases. Fig. 2(b) shows analogous results for aggregating value-option matrices. We observe that the transition point is near 3  $(\bar{p} \sim 3)$  for both the ranking and value-option matrix aggregation. However, the limit point

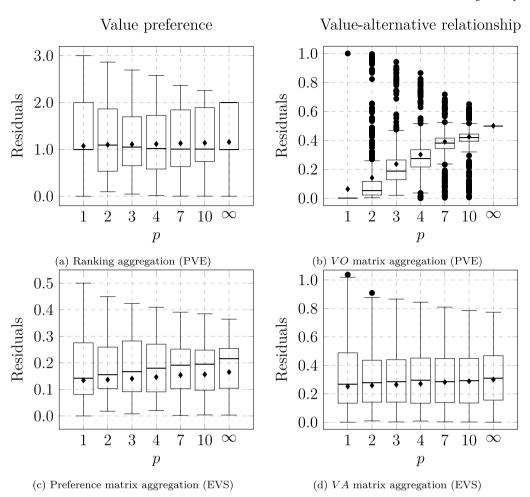


Fig. 3. Boxplots of residuals for different ethical principles in the value preference and value-alternative aggregation for the PVE (top) and EVS (bottom) case study. The diamond represents the mean and the circles represent the outliers.

varies for both cases ( $\hat{p} = 13$  for ranking aggregation and  $\hat{p} = 15$  for value-option matrix aggregation). This is because such points depend on the data of the problem.

The data dependency is corroborated when considering the EVS case. Figs. 2(c) and 2(d) plot the distance between consensuses for value preference matrix aggregation and values-action matrix aggregation, respectively. In these figures, we observe that the transition and limit points are different with respect to those computed for the PVE case. The transition point for value preference and value-action matrices aggregation is between 2 and 3, whereas the limit point is  $\hat{p} = 6$  in Fig. 2(c) and  $\hat{p} = 7$  in Fig. 2(d).

Therefore, a given ethical principle p can be interpreted as "more utilitarian" or "more egalitarian" depending on its relative position with respect to the transition point. However, notice that if the transition point  $\bar{p}$  turns out to be different for the two aggregations that we perform to compute a consensus value system, then if we choose the same ethical principle p to apply to both aggregations, it may lay in different regions.

#### 6.3.1. Takeaways for decision-makers

The comparison between the two case studies shows that the regions characterising the space of ethical principles depend on the domain and the data. Hence, a decision-maker must carefully examine the different ethical principles zones when choosing the ethical principle p. The decision-maker may desire to choose an ethical principle that leads to either utilitarian or egalitarian consensus for both aggregations (value preferences and value interpretations). However, the same value of parameter p could fall into different zones for moral value preferences

and moral value-alternatives relationships aggregation. This motivates the need for characterising the *joint* utilitarian and egalitarian zones for value preferences and value-alternatives relationship aggregations before choosing an ethical principle.

The visual analysis displayed in Fig. 2 intends to provide useful guidance for decision-makers concerned with obtaining a consensus on different value systems following an ethical principle of choice. In general, we propose the following guidelines:

- 1. Plot the distance between consensuses, as we do in Fig. 2.
- Plot the utilitarian, egalitarian, and fully egalitarian zones for value preference aggregation and values-alternatives relationship aggregation.
- Compute the joint utilitarian and egalitarian zones for both value preference and value-alternative relationship. For instance, in the PVE case study (the case for EVS is analogous), we define:
  - $[1, \bar{p}_m)$ , where  $\bar{p}_m = min(\bar{p}_R, \bar{p}_{VO})$ , as the joint utilitarian zone;
  - $(\bar{p}_M, \infty)$ , where  $\bar{p}_M = max(\bar{p}_R, \bar{p}_{VO})$ , as the joint egalitarian zone;
  - $[\bar{p}_m, \bar{p}_M]$  as a *mixed* zone that contains ethical principles that lie in different zones considering the consensus of ranking and value-option matrices.

After following the steps above, we obtain a *joint* space of ethical principles, which is partitioned into three zones of ethical principles:

- Utilitarian: ethical principles for which consensus on value preferences and value-alternatives relationship aggregation are both utilitarian.
- Egalitarian: ethical principles for which consensus on value preferences and value-alternatives relationship are both egalitarian.
- Mixed: ethical principles for which consensus on value preferences and value-alternatives relationship aggregation are not aligned (one is utilitarian, whereas the other is egalitarian).

This joint ethical principle space provides the decision-maker with the necessary information on choosing an ethical principle p to compute the consensus.

#### 6.4. The relationship between consensus and individual value systems

In Sections 6.1 and 6.2, we showed that the choice of the ethical principle impacts the resulting consensus value system. A further *microlevel* analysis helps us investigate how the relationship between the consensus and the individual value systems change as the ethical principle changes. Such a micro-level analysis helps quantify the tradeoff when moving away from the majority (utilitarian case) to include the minority (egalitarian case). This analysis complements the one conducted in Section 6.3 (when characterising ethical principles) to help the policymaker choose the ethical principle to employ when aggregating value systems.

In what follows, we analyse the distribution of *residuals*, which represent the *gap* between given consensus value systems and the individual value systems aggregated to obtain the consensus. For instance, when considering the PVE case study,  $|R_i[v] - R_S[v]|$  yields the residual for the ranking of individual value system *i* with respect to the consensus value system regarding value *v*. Analogously, we can also calculate the residual for the value-option matrix of individual value system *i* ( $|VO_i[v, o] - VO_S[v, o]|$ ). Fig. 3 plots the distribution of the residuals obtained when computing consensus value systems for both case studies as the value of the ethical principle (*p*) increases.

First, we focus on the PVE case study. Figs. 3(a) and 3(b) plot the distributions of the residuals for the ranking aggregation and the VO-matrix aggregation, respectively. In Fig. 3(a), we observe that the utilitarian ethical principle (p = 1) yields the maximum residuals, hence confirming that the utilitarian principle considers less the individuals within the minority of society. As the value of parameter p increases towards the egalitarian principle, the maximum residuals decrease. For the egalitarian ethical principle ( $p = \infty$ ), we obtain that the maximum residual is 33% smaller than for the utilitarian principle (from 3.0 down to 2.0). This is because the egalitarian ethical principle aims to reduce the distance between the consensus and the most distant individuals of society. Further, we observe that the mean of the residuals gradually increases as the value of parameter p increases (up to an 8% increase for the egalitarian case). The observations above are more pronounced when we analyse the residual distribution for aggregating individual VO matrices using different ethical principles (Fig. 3(b)). On the one hand, the value of the maximum residual halves when moving from p = 1 (1.0) to  $p = \infty$  (0.5). On the other hand, the mean of the residuals dramatically increases from a value close to 0 until reaching 0.5 for the egalitarian case ( $p = \infty$ ), which amounts to a x7 increase of the mean.<sup>9</sup>

We confirm the observations above when analysing the EVS case study. Figs. 3(c) and 3(d) show the distribution of residuals for the aggregation of individual preference matrices  $P_i$  and the aggregation of individual value-action matrices  $VA_i$ , respectively for the weighted scenario (different social influences per country). On the one hand, the maximum residual decreases as we increase p for both preference matrix and value-action matrix aggregations. On the other hand, there is a smooth increase of the mean of the residuals as we increase p for both the preference matrix and value-action matrix aggregations. However, the values of residuals differ compared to the PVE case. This is due to the differences in each case study's set of individual value systems.

#### 6.4.1. Takeaways for decision-makers

Our analysis shows that moving away from the majority (utilitarian) to include the minority (egalitarian) leads to an increase in the mean of the residuals and a decrease in the maximum residuals. While the guidelines provided in Section 6.3.1 specify macro-directives for choosing the ethical principle p, the analysis of residuals gives concrete information about the trade-offs between choosing different ethical principles. The decision-maker must weigh the extent to which the increase in the average residual of a large portion of individuals compensates for minimising the distance to the minority (when moving from utilitarian to egalitarian principle).

#### 7. Conclusions and future work

The main contribution of this paper is to provide novel computational means and guidelines for a decision-maker to conduct a principled aggregation of value systems. This is a fundamental step towards designing AI systems that align with a group of individuals with different value systems, namely, towards addressing the *pluralistic value alignment* problem defined by Gabriel [6]. Our contributions make headway to developing trustworthy AI [2] systems that adhere to ethical principles and values.

We show that the problem of computing a consensus value system can be cast as an  $\ell_p$ -regression [45] (or norm approximation [46]) problem. By doing so, we provide a principled and general theoretical framework to solve the above-mentioned problem for a range of ethical principles—from utilitarian (maximum utility) to egalitarian (maximum fairness)—in a scalable and reliable way, thanks to recent results in the machine learning literature [45]. Importantly, our approach also allows us to compute the consensus for *any* single value of *p*, which was not possible before for the generator of social choice functions that we employ (González-Pachón and Romero [44] can only deal with p = 1and  $p = \infty$ ).

We study the aggregation of value systems using real-world data from two case studies: the Participatory Value Evaluation (PVE) [41] process and the European Values Study (EVS) [42]. Our empirical evaluation of the case studies draws insights for a decision-maker about how to employ our computational tools to perform value system aggregation. In particular, we show how to proceed to: (i) quantify the impact of choosing different ethical principles on the resulting consensus value system; (ii) characterise the semantics of the available ethical principles (to determine whether a given ethical principle produces a consensus leaning towards the utilitarian or the egalitarian ethical principle); and (iii) quantify the trade-off when moving away from the majority to include the minority. Importantly, our observations vary per case study since they handle different value systems.

In this paper, we treat the aggregation of individual value systems. However, the aggregation must be preceded by the *estimation* of individual value systems [39]. To this end, surveys such as PVE and EVS can be employed to collect value-laden input from the participants, and methods like Siebert et al. [43] (Section 3.1.2) are employed to compound the survey answers into individual value systems. Such methods could be further automated using natural language processing to automatically detect the values that are motivating the survey answers [81,82]. Ultimately, the aggregation of value systems with the computation of a consensus value system.

<sup>&</sup>lt;sup>9</sup> Recall that value-option matrices are binary. We highlight that we obtain a consensus matrix full of zeros for the utilitarian principle (p = 1). Because the value-option matrices are binary, all the residuals are either 0 or 1. In fact, more than the 75% of the residuals are 0. As to the egalitarian principle ( $p = \infty$ ), we obtain a consensus matrix full of 0.5 values. Hence, all the residuals are 0.5.

As future work, we envision three research paths. First, we plan to generalise our framework so that each individual can choose their own ethical principle before aggregating value systems. This might call for developing new social choice functions and computational tools to account for multiple ethical principles. Second, we want to develop a community-oriented approach to aggregate value systems. As a first step, we would detect communities of individuals with similar value systems. This would allow us to compute the consensus value system per community and, ultimately, the aggregation of the value systems of all the communities. Finally, we plan to explore further connections with the literature on multi-expert decision-making (e.g., [49,50]). Indeed, the distance function employed in our paper can be regarded as a penalty function as defined in [83]. However, profiting from the aggregation functions proposed in that body of work would require investigating their social choice properties. Although this challenge demands additional work beyond this paper's scope, we believe it is worth exploring whether we can benefit from using penalty functions with lower computational costs.

## CRediT authorship contribution statement

**Roger X. Lera-Leri:** Writing – review & editing, Writing – original draft, Software, Methodology, Data curation, Conceptualization. **Enrico Liscio:** Writing – review & editing, Writing – original draft, Software, Methodology, Data curation, Conceptualization. **Filippo Bistaffa:** Writing – review & editing, Software, Methodology, Conceptualization. **Catholijn M. Jonker:** Writing – review & editing, Funding acquisition. **Maite Lopez-Sanchez:** Writing – review & editing, Writing – original draft, Methodology. **Pradeep K. Murukannaiah:** Writing – review & editing, Methodology. **Juan A. Rodriguez-Aguilar:** Writing – review & editing, Writing – original draft, Methodology. **Funding acquisition**, Formal analysis. **Francisco Salas-Molina:** Writing – review & editing, Methodology.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Data availability

Data will be made available on request.

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Knowledge-Based Systems 287 (2024) 111453

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